

Corrigendum to "Some new identities for Schur functions"

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Theorem 5 of [1, p. 496] is not stated correctly. For completeness, here are the correct statements.

Theorem 5. For non negative integers m and n ,

$$\sum_{\lambda \subseteq (m^n)} f_\lambda(a, b) s_\lambda(X) = \sum_{\xi \in \{\pm 1\}^n} \beta(\xi, a, b) \prod_i x_i^{m(1-\xi_i)/2}$$

where the coefficient $\beta(\xi, a, b)$ is equal to

$$\begin{cases} \frac{a^m D(\xi, b)}{1 - a^{-1}b} \Phi(X^\xi; a^{-1}, b) + \frac{b^m D(\xi, a)}{1 - ab^{-1}} \Phi(X^\xi; a, b^{-1}) & \text{if } |\xi|_{-1} \text{ odd,} \\ \frac{D(\xi, ab)}{1 - ab} \Phi(X^\xi; a, b) + \frac{(ab)^m D(\xi, 1)}{1 - a^{-1}b^{-1}} \Phi(X^\xi; a^{-1}, b^{-1}) & \text{if } |\xi|_{-1} \text{ even.} \end{cases}$$

Indeed, the second paragraph of the page 505 of [1] should be read as follows :
In the same way, we find for any even size subset $Y \subseteq X$ that

$$d(Y) = -\frac{D(\xi, 1)}{1 - a^{-1}b^{-1}} \Phi(X^\xi; a^{-1}, b^{-1})$$

and for any odd size subset $Y \subseteq X$ that

$$\begin{aligned} a(Y) &= \frac{D(\xi, b)}{1 - a^{-1}b} \Phi(X^\xi; a^{-1}, b), \\ b(Y) &= -\frac{D(\xi, a)}{1 - ab^{-1}} \Phi(X^\xi; a, b^{-1}). \end{aligned}$$

Consequently, the first paragraph of the page 506 of [1] should be read as follows :
On the other hand, we have

$$\begin{aligned} \beta(\xi, 1, 0) &= \Phi(X^\xi; 1, 0), \\ \beta(\xi, 1, -1) &= \begin{cases} \Phi(X^\xi; 1, -1) & \text{if } m \text{ even,} \\ \Phi(X^\xi; 1, -1) \prod_i x_i^{(\xi_i-1)/2} & \text{if } m \text{ odd;} \end{cases} \end{aligned}$$

and

$$\beta(\xi, 0, 0) = \begin{cases} 0 & \text{if } |\xi|_{-1} \text{ is odd,} \\ \Phi(X^\xi; 0, 0) & \text{otherwise.} \end{cases}$$

We thank Masao Ishikawa for carefully checking our theorem and pointing out the above mistake.

References

- [1] F. Jouhet and J. Zeng, Some new identities for Schur functions, Adv. in Appl. Math. 27 (2001), no. 2-3, 493–509.