

Cell Dynamics and Complex Systems

An overview of case studies

Samuel Bernard 01.02.2023

DYNAMICS OF TUMOR GROWTH

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Gompertz equation of the following form:

$$W/W_0 = e^{\frac{A}{\alpha}(1-e^{-\alpha t})}$$

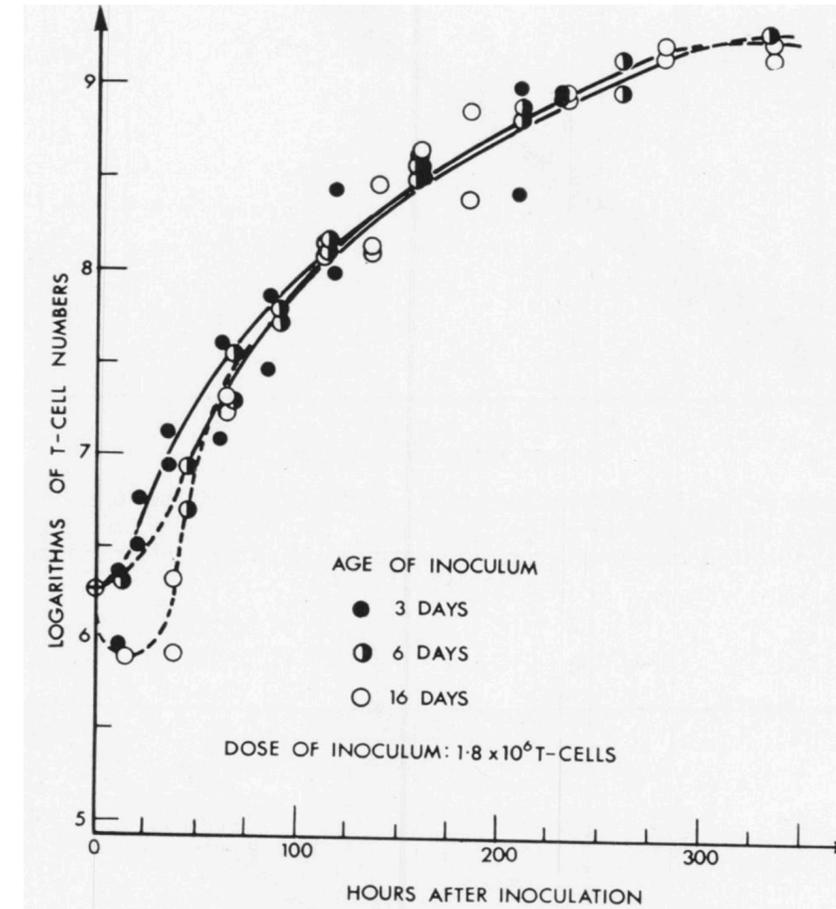


TABLE II.—*Analysis of Theoretical Gompertz Functions in Terms of Doublings*

Gompertz curve Corresponding to :	Duration, initial doubling,	Ratio, second to first doubling time	Approx. No. doublings to upper limit
Krebs	3.26 hours	1.06	18
Ehrlich	9.26 hours	1.10	12
MC ₁ M, low dose	6.09 hours	1.11	11
6C ₃ HED, high dose	19.6 hours	1.44	4.5
6C ₃ HED, low dose	11.9 hours	1.19	7.5
DBA lymphoma	2.59 hours	1.07	16
E1 ₄ , low dose	3.46 hours	1.08	15
E1 ₄ , high dose	4.23 hours	1.12	10
EO771	1.08 days	1.09	15
Osteosarcomas	5.03 days	1.15	9
Walker, W26b1	3.26 days	1.08	14
Walker, W12a7	2.07 days	1.05	23
Walker, W10a6	1.99 days	1.09	13
Walker, W10b4	5.29 days	1.02	62
R39, R3a7	0.56 days	1.08	14
R39, R4c4	1.35 days	1.13	9.5
R39, a7R3	0.97 days	1.07	16
Flexner-Jobling	1.84 days	1.11	11
Brown-Pearce	0.576 days	1.12	10

Inequality of Mean Interdivision Time and Doubling Time

By P. R. PAINTER AND A. G. MARR

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The mean interdivision time $\bar{\tau}$ is then

$$\int_0^{\infty} \tau f(\tau) d\tau.$$

$$\bar{\tau} = \ln 2/k, \quad \bar{\tau} \approx \ln 2/k + k\sigma^2/2,$$

Organism	Standard deviation, σ (min.)	Specific growth rate, k (min. ⁻¹)	$\ln 2/k$ (min.)	$\bar{\tau}$, observed (min.)	$\bar{\tau}$, estimated (min.)
<i>Pseudomonas aeruginosa</i>	5.37	0.01831*	37.85	38.1	38.11
<i>Bacillus megaterium</i>	7.76	0.03259†	21.27	22.3	22.25
<i>Bacillus mycoides</i>	14.2	0.02637*	26.29	28.7	28.95

Global Geometry of the Stable Regions for Two Delay Differential Equations

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$$\dot{x}(t) + ax(t) + bx(t-r) + cx(t-\sigma) = 0, \quad r \geq 0, \sigma \geq 0, t \geq 0$$

$$p(\lambda, r, \sigma) \stackrel{\text{def}}{=} \lambda + a + be^{-\lambda r} + ce^{-\lambda \sigma} = 0.$$

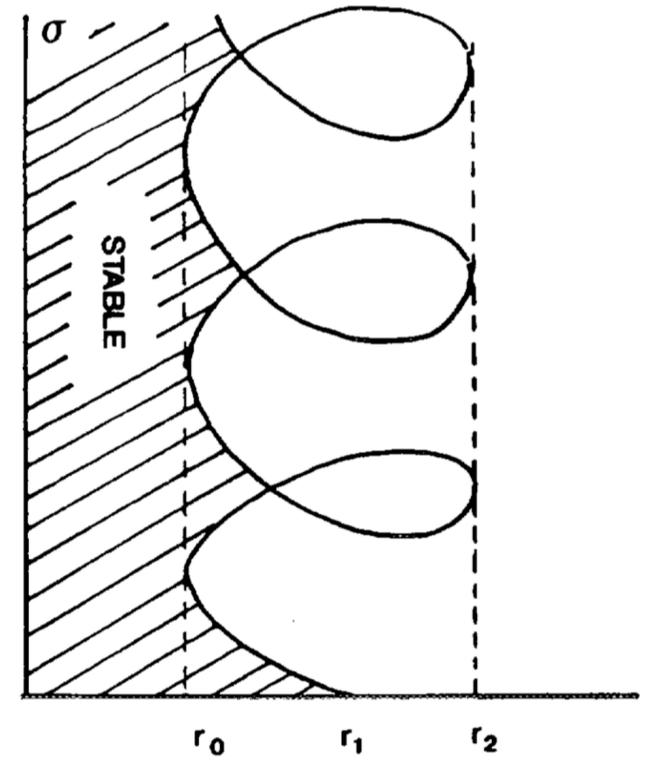


FIGURE 3.7

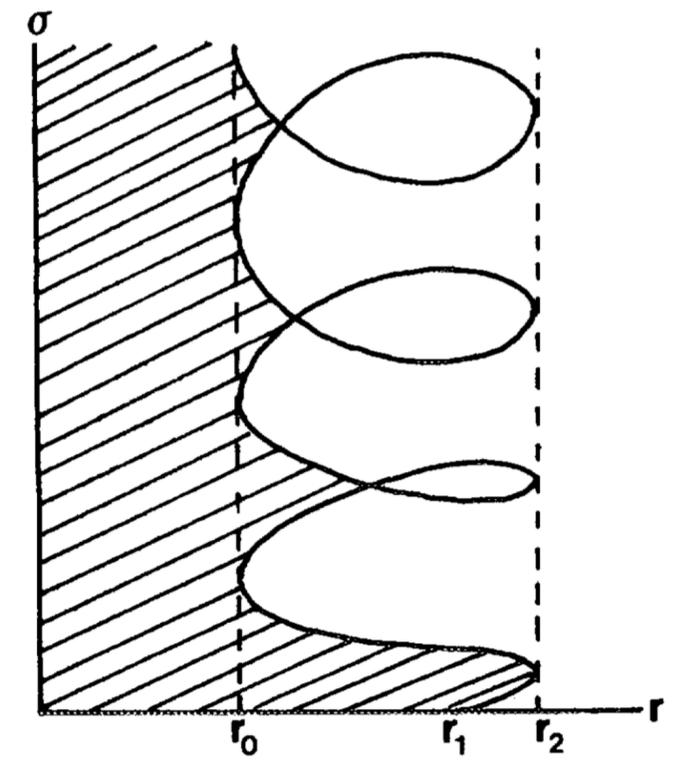
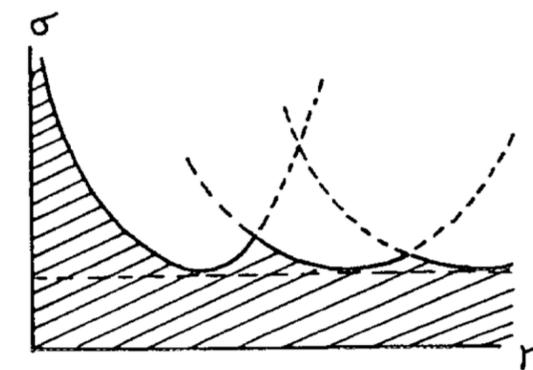
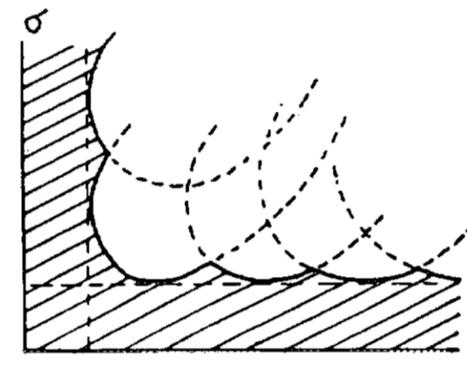


FIGURE 3.8



A nonlinear structured population model of tumor growth with quiescence

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² Vanderbilt University, Department of Mathematics, Nashville, TN 37235, USA

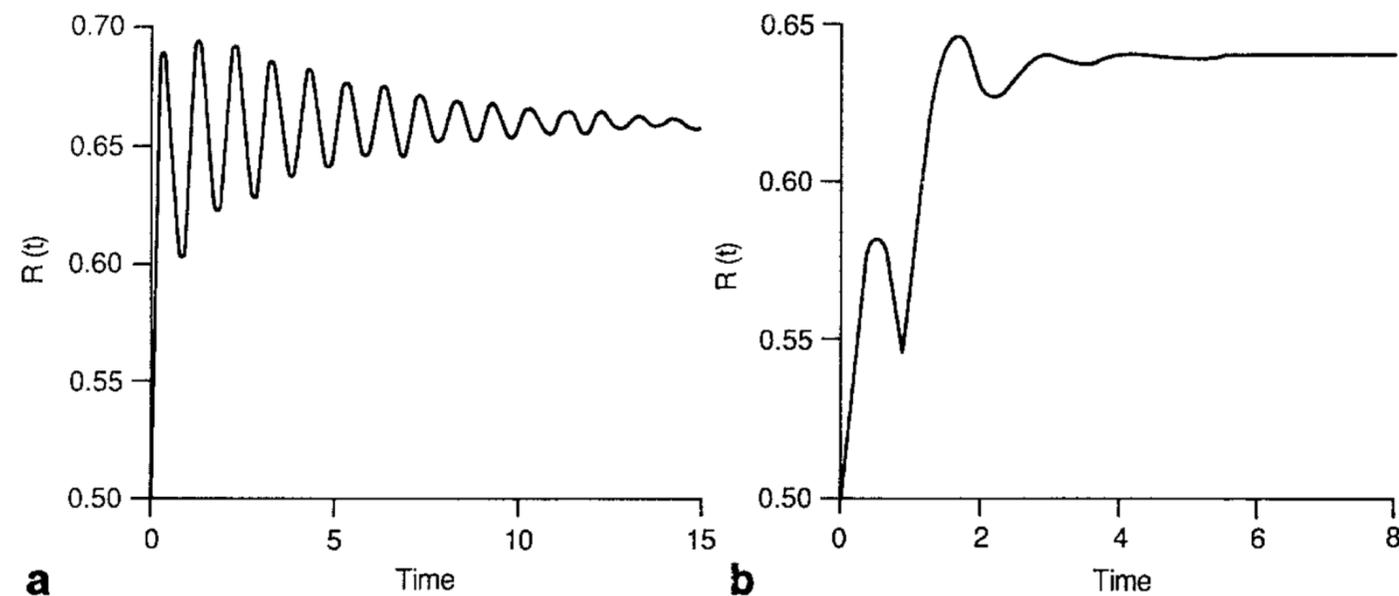
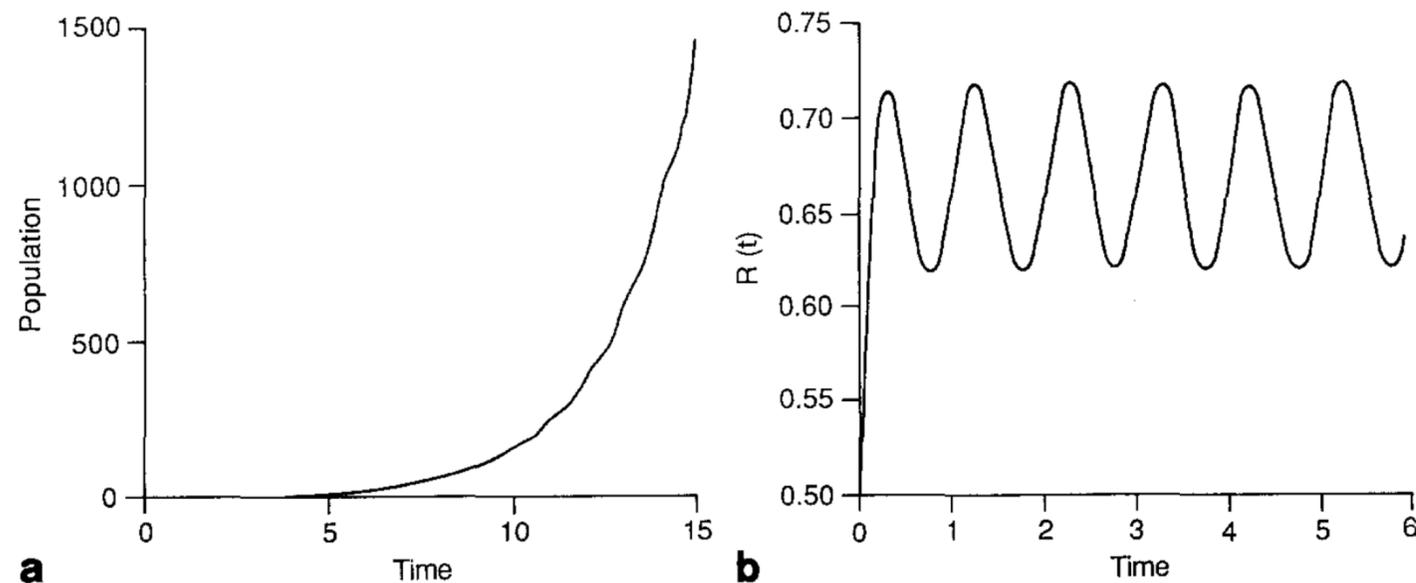
$$(2.1) \quad \frac{\partial}{\partial t} p(x, t) + \frac{\partial}{\partial x} (g(x)p(x, t)) = 2(2 - r(x, N(t)))b(2x)p(2x, t) - b(x)p(x, t) - \mu_p(x)p(x, t) + \varrho(x, N(t))q(x, t),$$

$$t > 0, \quad \frac{x_0}{2} < x < x_1,$$

$$(2.2) \quad \frac{\partial}{\partial t} q(x, t) = 2r(x, N(t))b(2x)p(2x, t) - \mu_q(x)q(x, t) - \varrho(x, N(t))q(x, t), \quad t > 0, \quad \frac{x_0}{2} < x < \frac{x_1}{2},$$

$$(2.3) \quad p\left(\frac{x_0}{2}, t\right) = 0, \quad t > 0,$$

$$(2.4) \quad p(x, 0) = \phi(x), \quad \frac{x_0}{2} < x < x_1, \quad q(x, 0) = \psi(x), \quad \frac{x_0}{2} < x < \frac{x_1}{2}.$$



CHAOTIC DYNAMICS IN A SIMPLE PREDATOR-PREY MODEL WITH DISCRETE DELAY

GUIHONG FAN

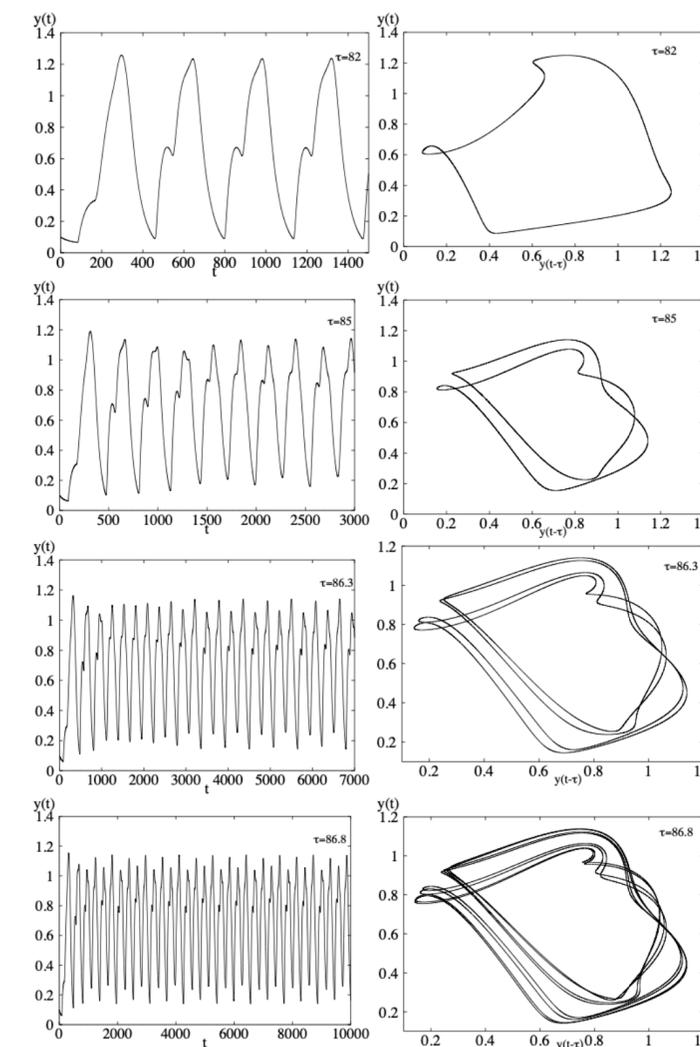
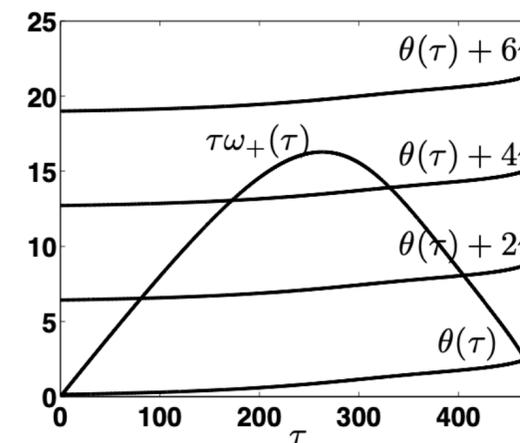
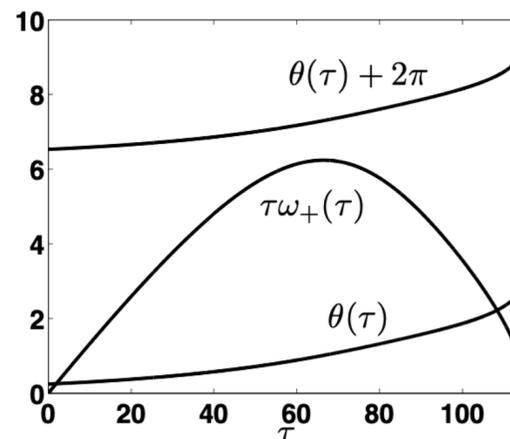
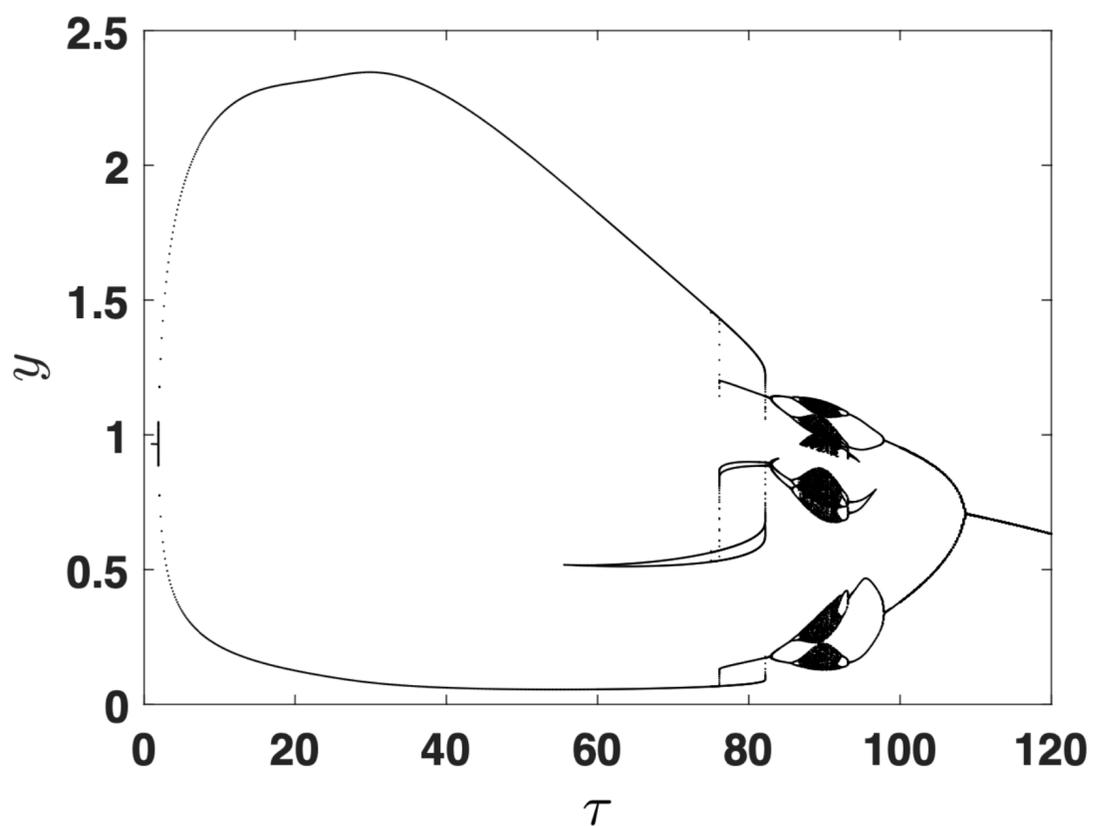
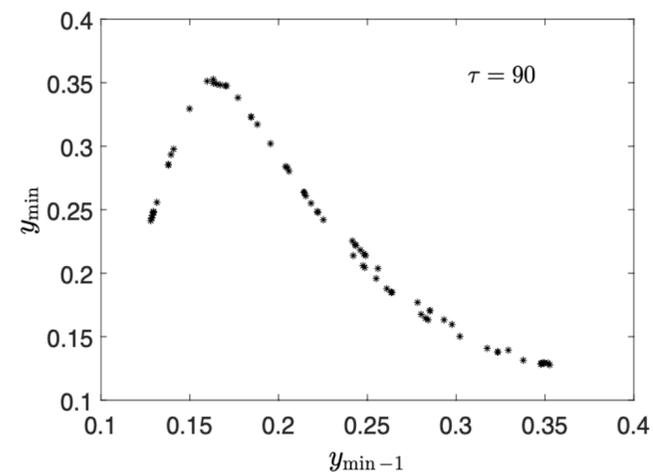
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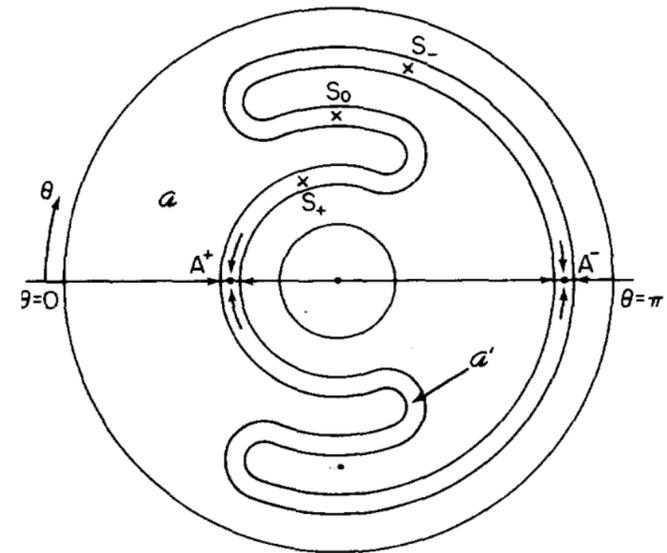
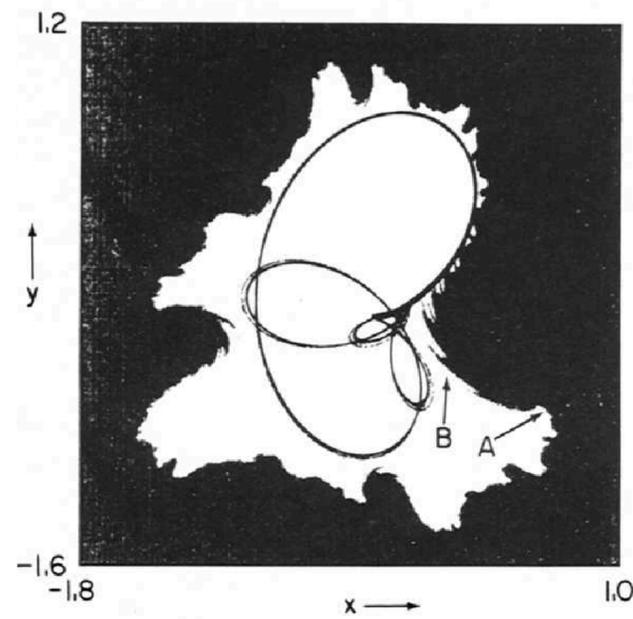
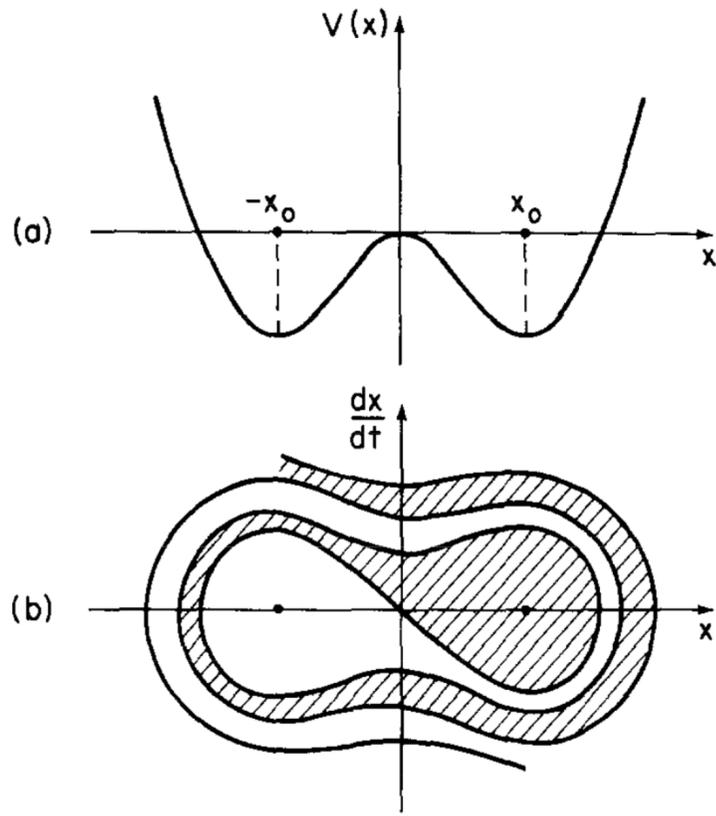
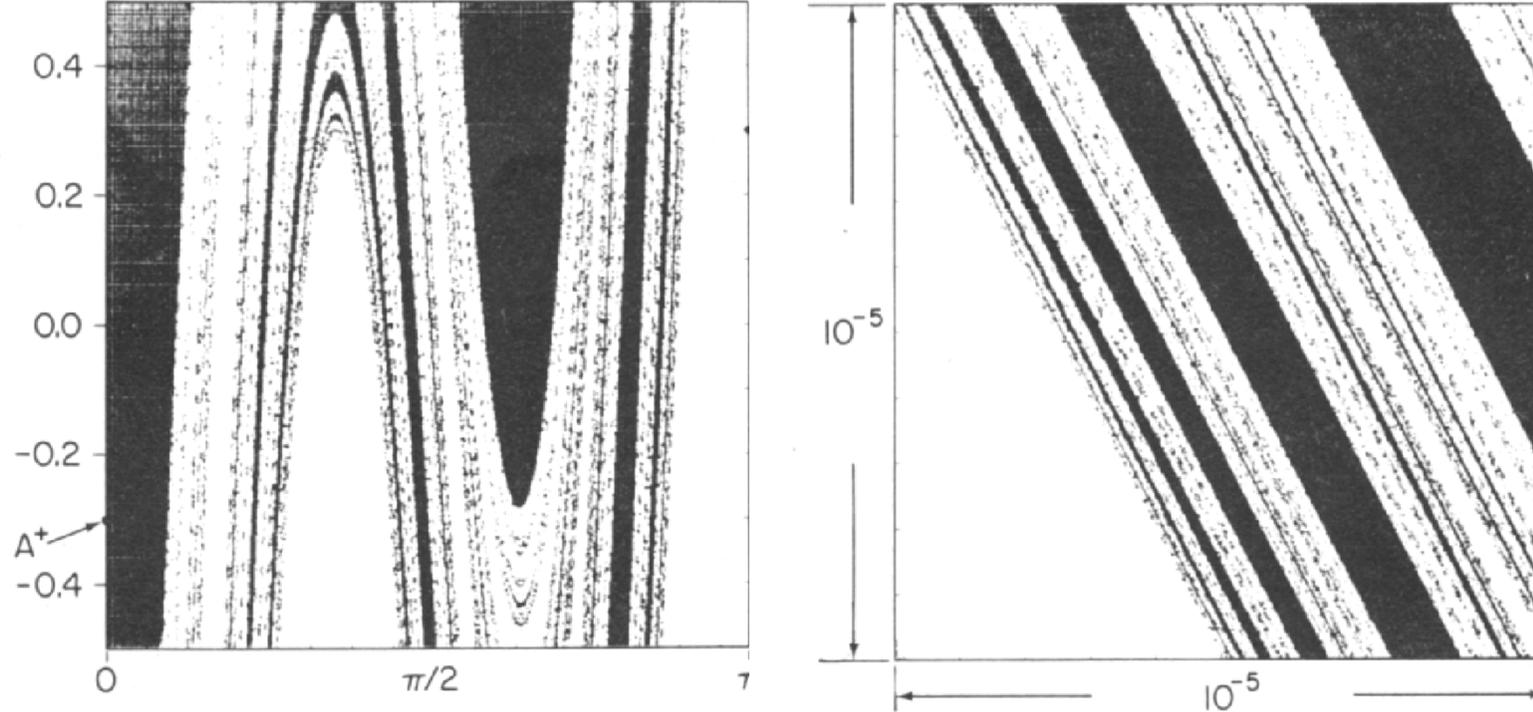
$$\begin{cases} \dot{x}(t) = rx(t) \left(1 - \frac{x(t)}{K}\right) - my(t)x(t), \\ \dot{y}(t) = -sy(t) + Ye^{-s\tau}my(t-\tau)x(t-\tau). \end{cases}$$

$$(\lambda + s)(\lambda + y^* - (1 - 2x^*)) + Ye^{-(s+\lambda)\tau}x^*(1 - 2x^*) - \lambda Ye^{-(s+\lambda)\tau}x^* = 0.$$



FRACTAL BASIN BOUNDARIES

Steven W. McDONALD,^a Celso GREBOGI,^a Edward OTT^{a,b} and James A. YORKE^c

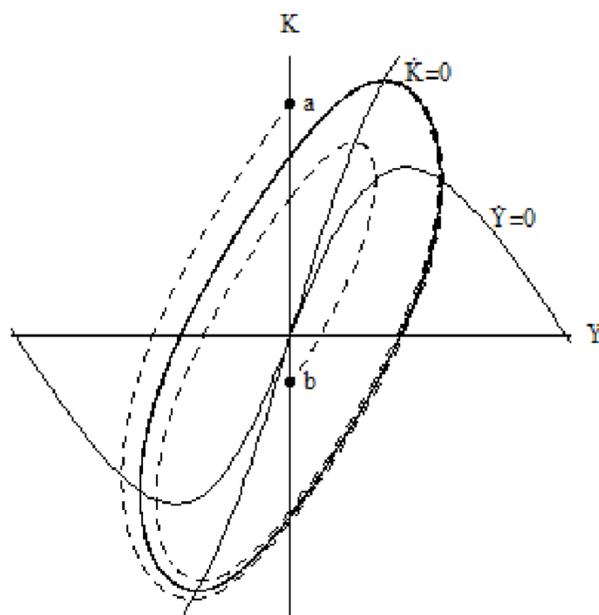


Delay Differential Nonlinear Economic Models*

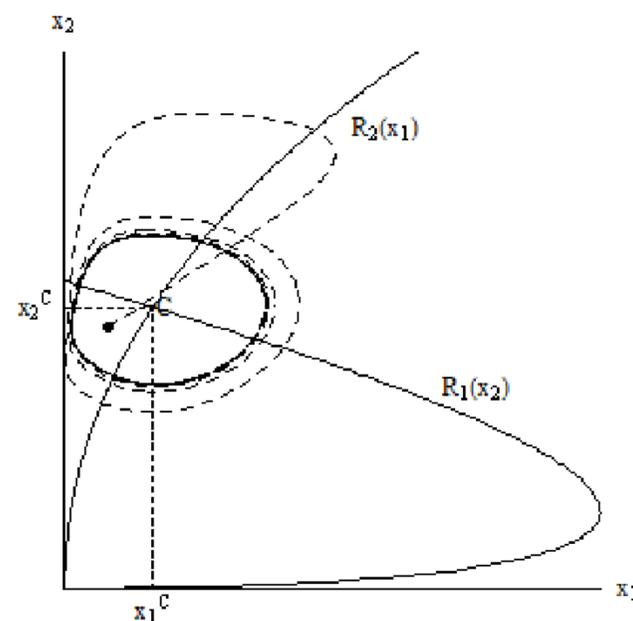
Akio Matsumoto[†]
Chuo University

Ferenc Szidarovszky[‡]
University of Arizona

$$\begin{cases} \dot{Y}(t) = \alpha [I(Y(t), K(t)) - S(Y(t))], \\ \dot{K}(t) = I(Y(t - \theta), K(t)) - \delta K(t), \end{cases}$$

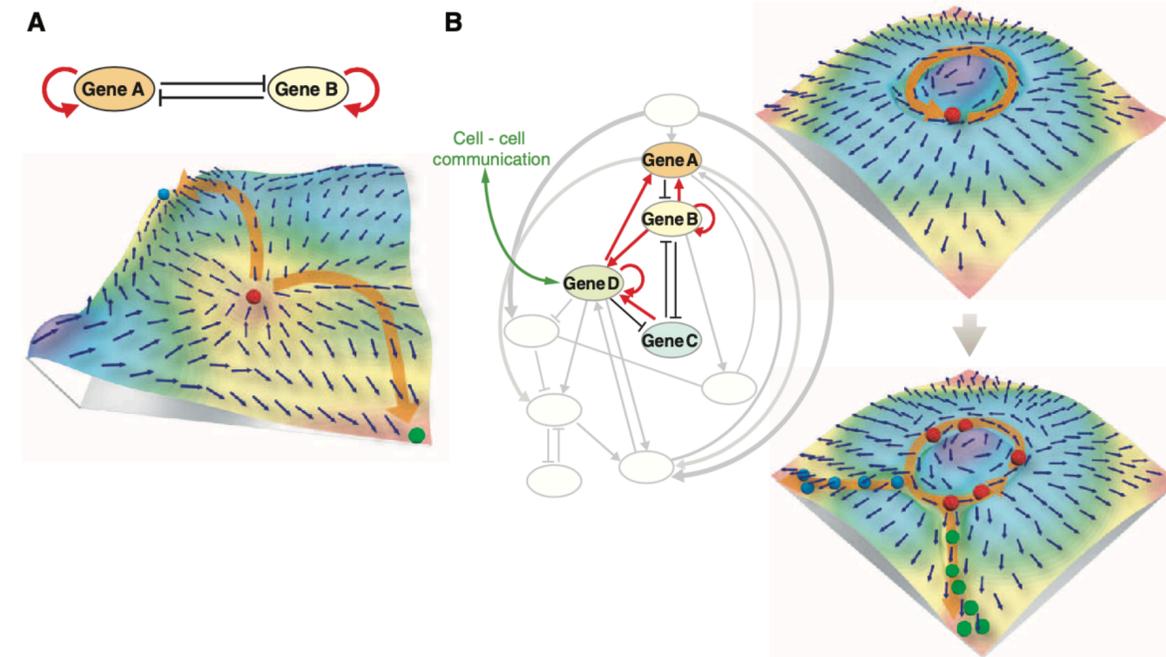
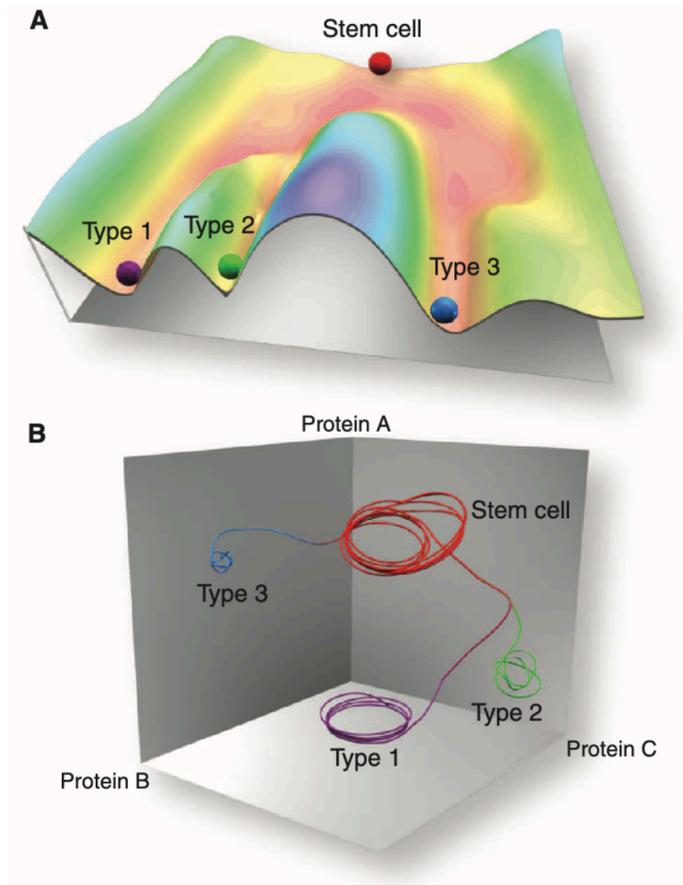


$$\begin{cases} \dot{x}_1(t) = k_1 \{R_1(x_2(t - \theta_1)) - x_1(t)\}, \\ \dot{x}_2(t) = k_2 \{R_2(x_1(t - \theta_2)) - x_2(t)\}, \end{cases}$$



A Dynamical-Systems View of Stem Cell Biology

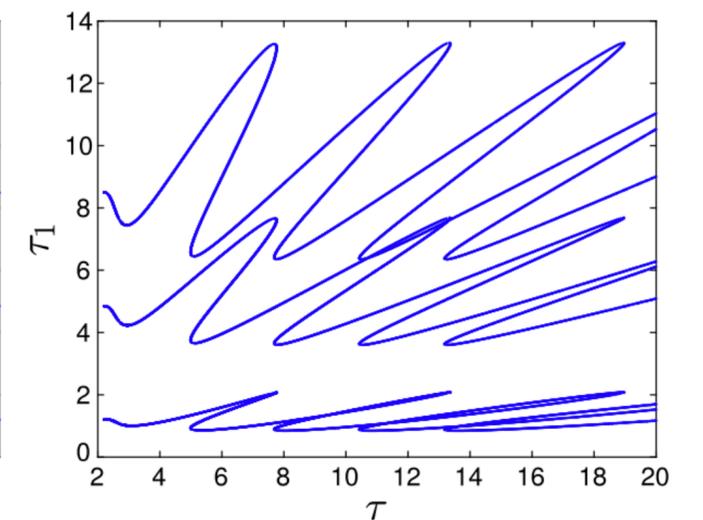
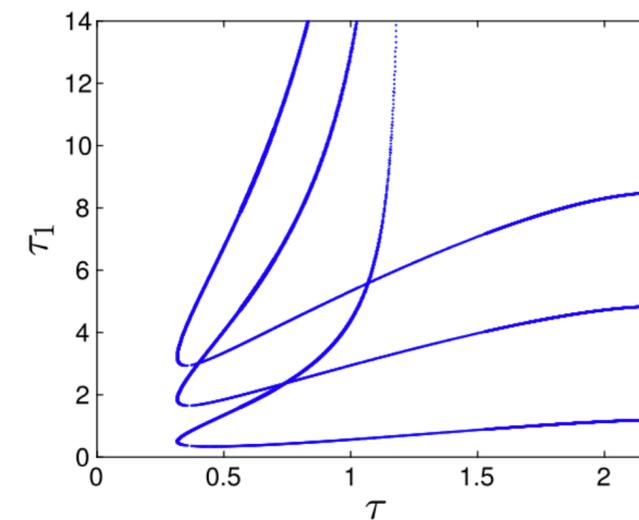
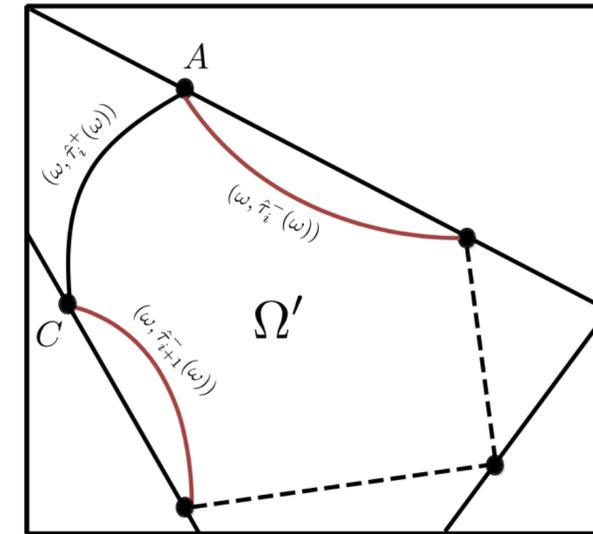
Chikara Furusawa¹ and Kunihiko Kaneko^{2*}



Geometric stability switch criteria in delay differential equations with two delays and delay dependent parameters [☆]

Qi An ^a, Edoardo Beretta ^b, Yang Kuang ^c, Chuncheng Wang ^a,
Hao Wang ^{d,*}

$$D(\lambda, \tau, \tau_1) := P_0(\lambda, \tau) + P_1(\lambda, \tau)e^{-\lambda\tau} + P_2(\lambda, \tau)e^{-\lambda\tau_1} = 0,$$



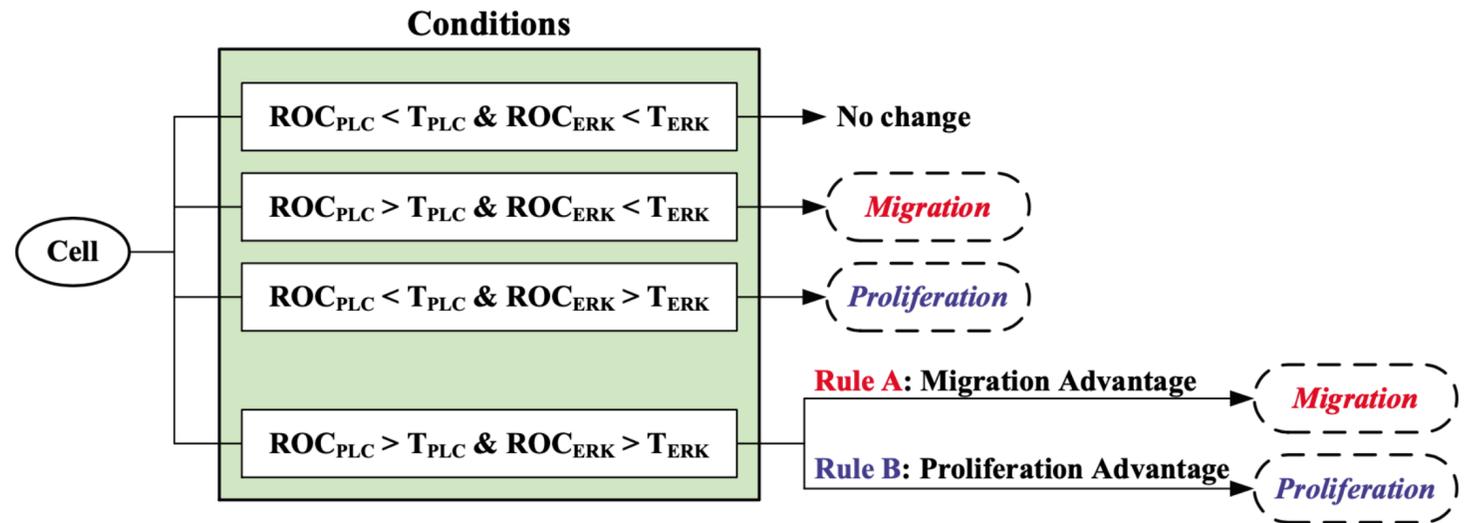
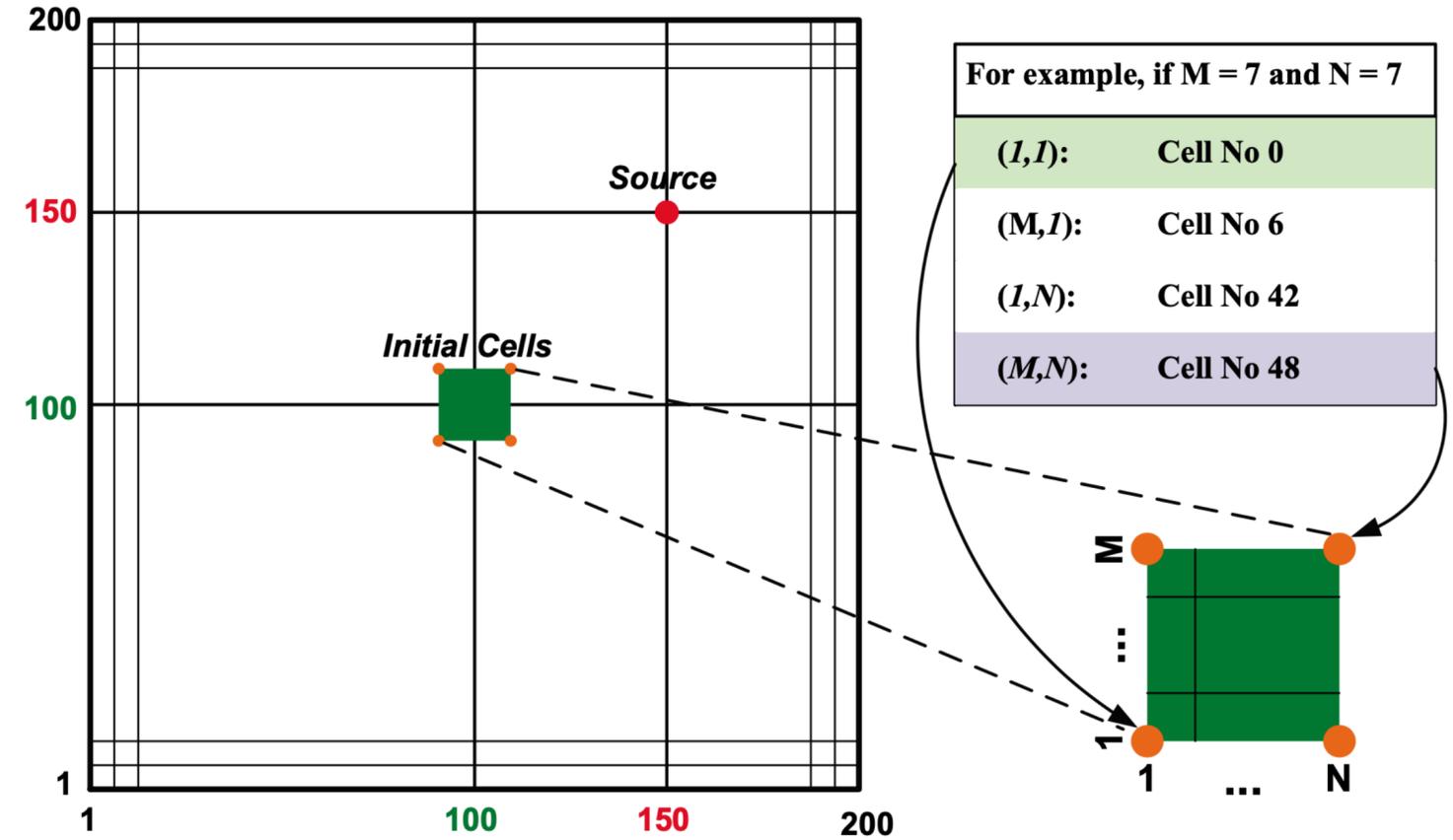
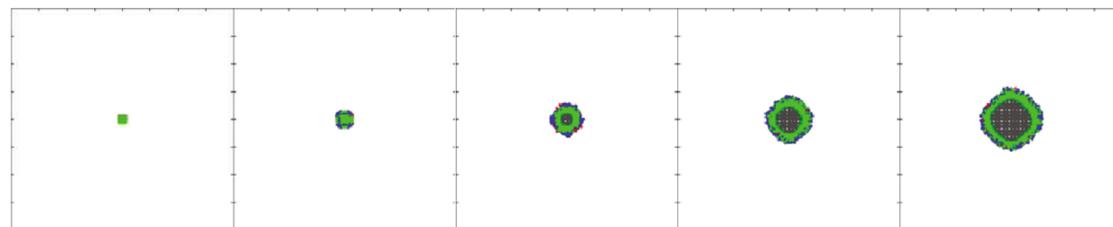
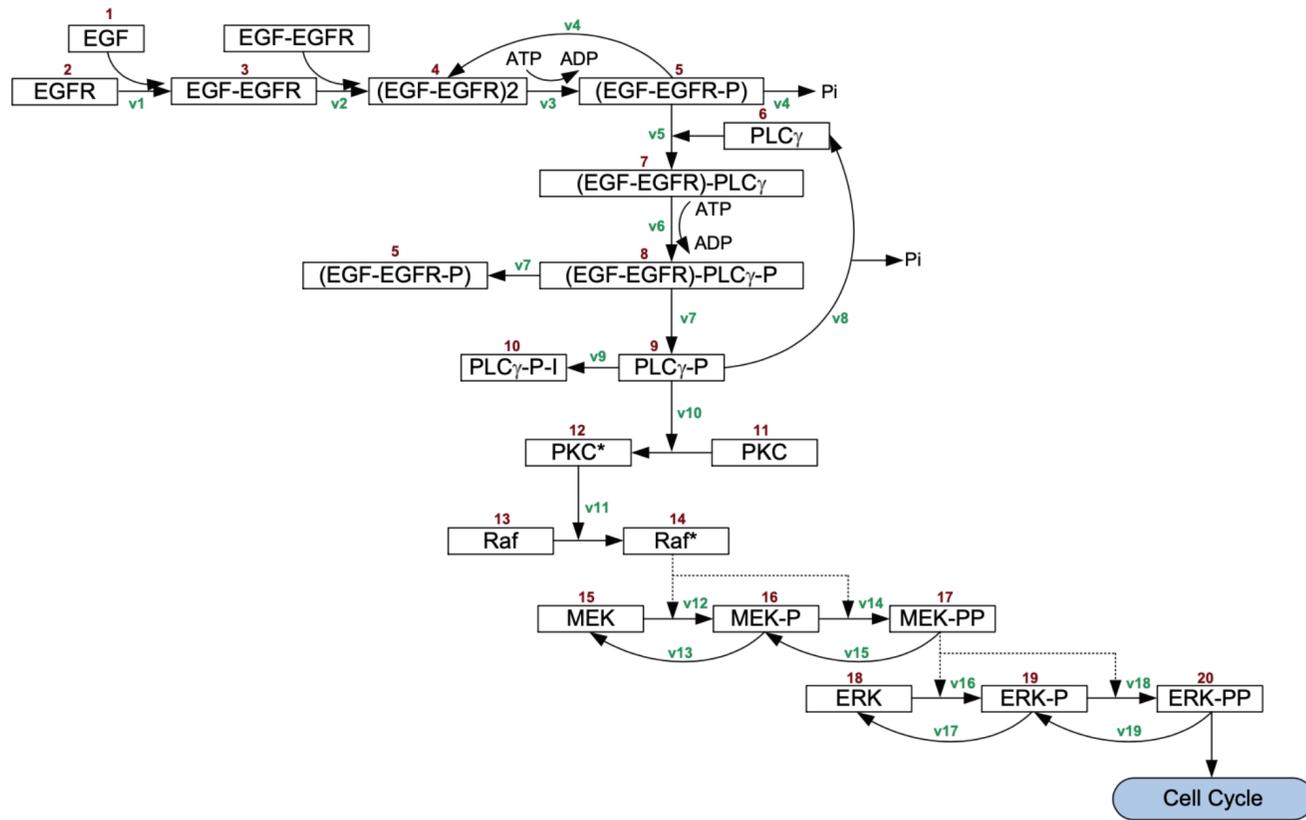
Theoretical Biology and Medical Modelling

Research

Simulating non-small cell lung cancer with a multiscale agent-based model

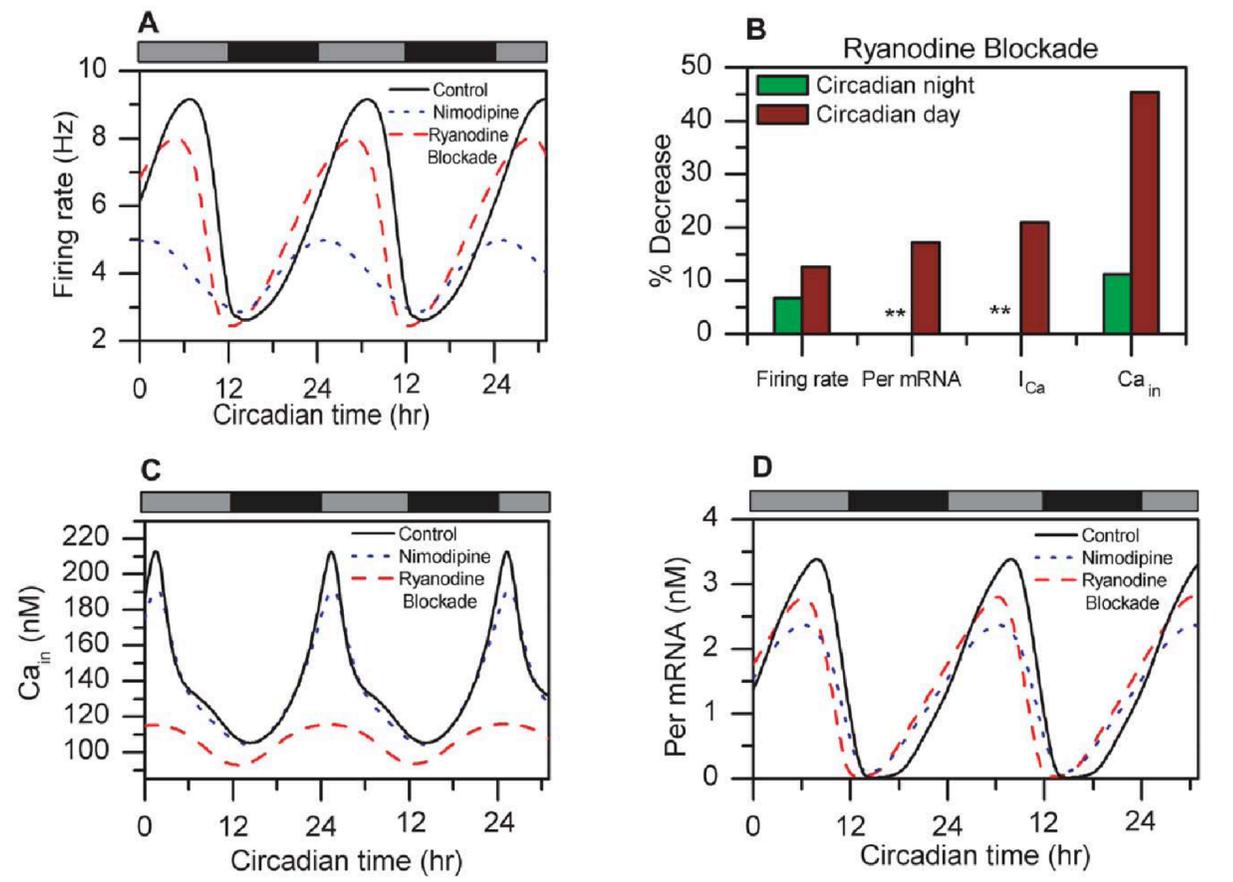
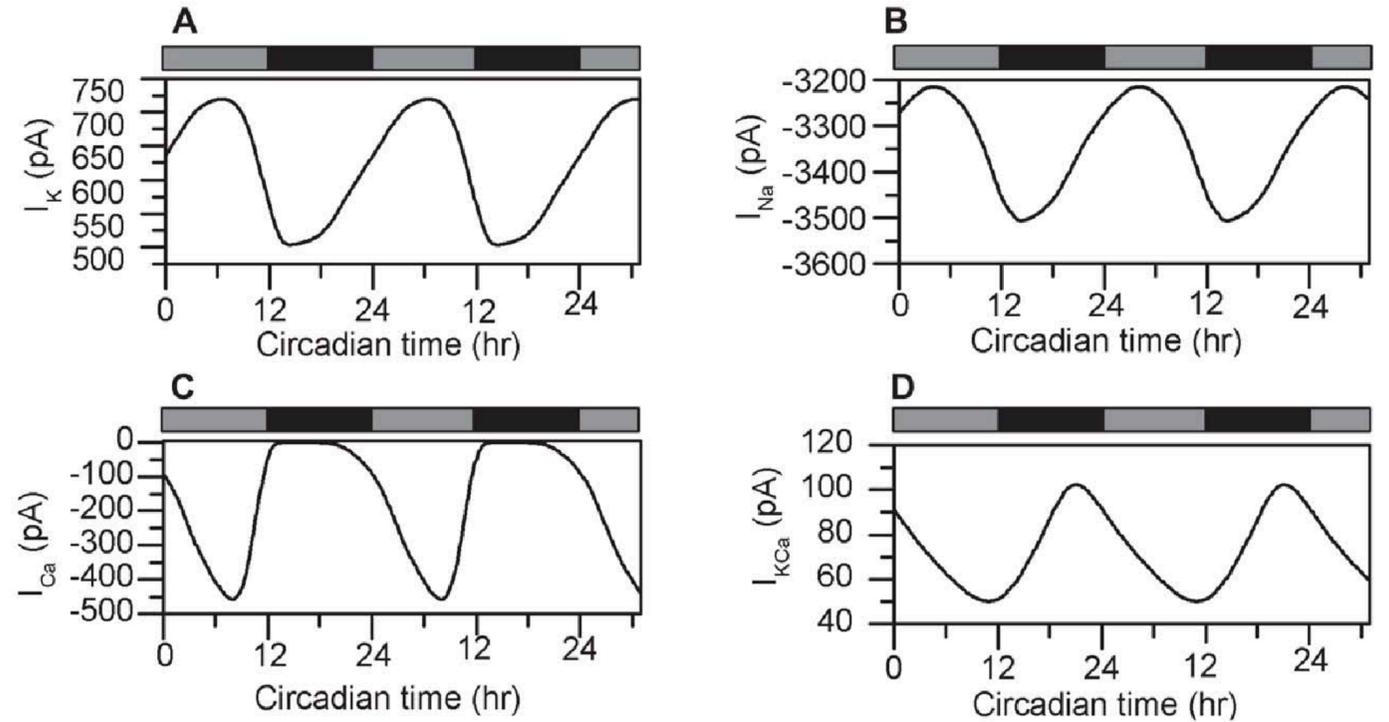
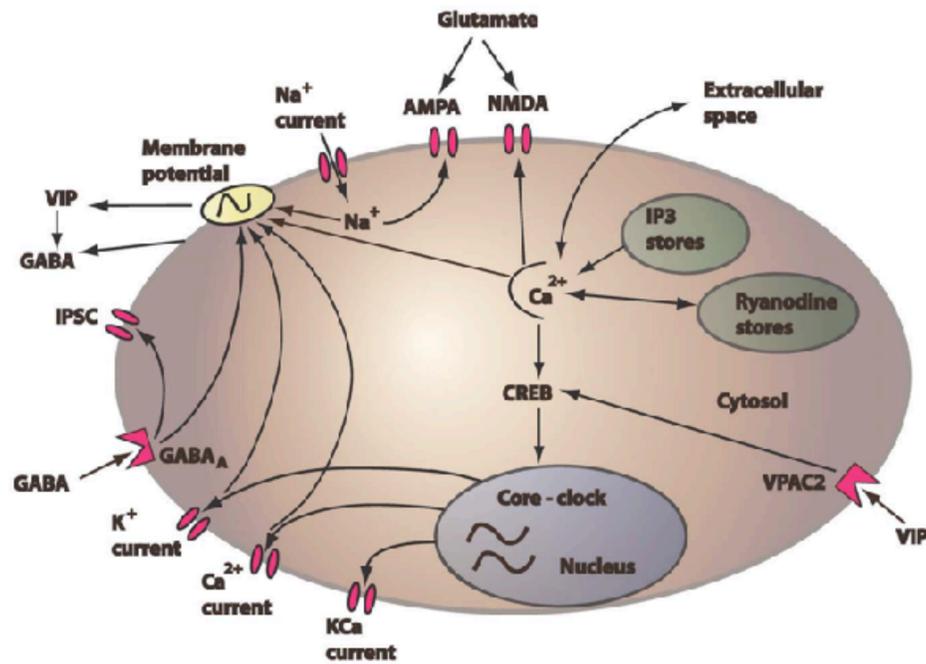
Zhihui Wang, Le Zhang, Jonathan Sagotsky and Thomas S Deisboeck*

Open Access



A Multiscale Model to Investigate Circadian Rhythmicity of Pacemaker Neurons in the Suprachiasmatic Nucleus

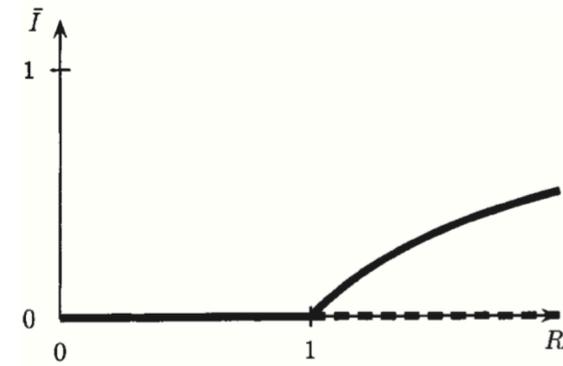
Christina Vasalou, Michael A. Henson*



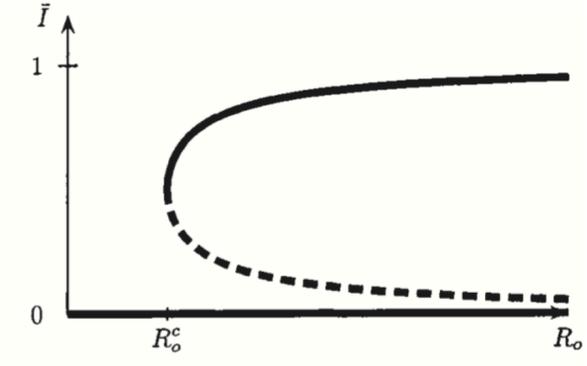
P. van den Driessche · James Watmough

A simple SIS epidemic model with a backward bifurcation

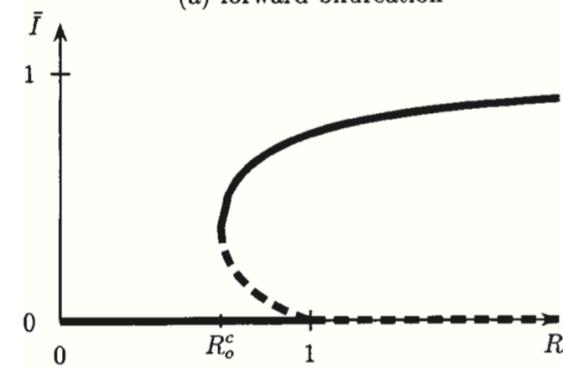
$$I(t) = I_o(t) + \int_0^t \lambda(I(u))I(u)(1 - I(u))P(t - u)e^{-b(t-u)} du,$$



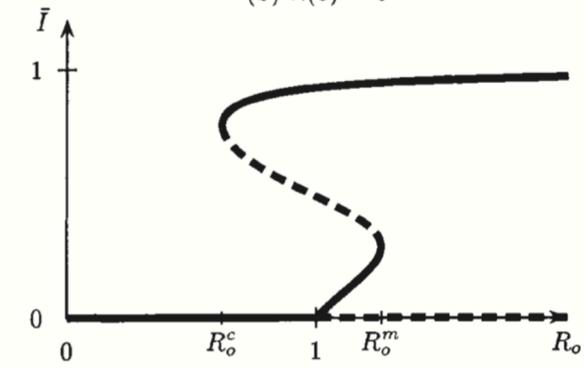
(a) forward bifurcation



(b) $\lambda(0) = 0$



(c) backward bifurcation



(d) forward bifurcation with hysteresis

Spontaneous Synchronization of Coupled Circadian Oscillators

Didier Gonze,^{*†} Samuel Bernard,^{*} Christian Waltermann,^{*} Achim Kramer,[‡] and Hanspeter Herzel^{*}

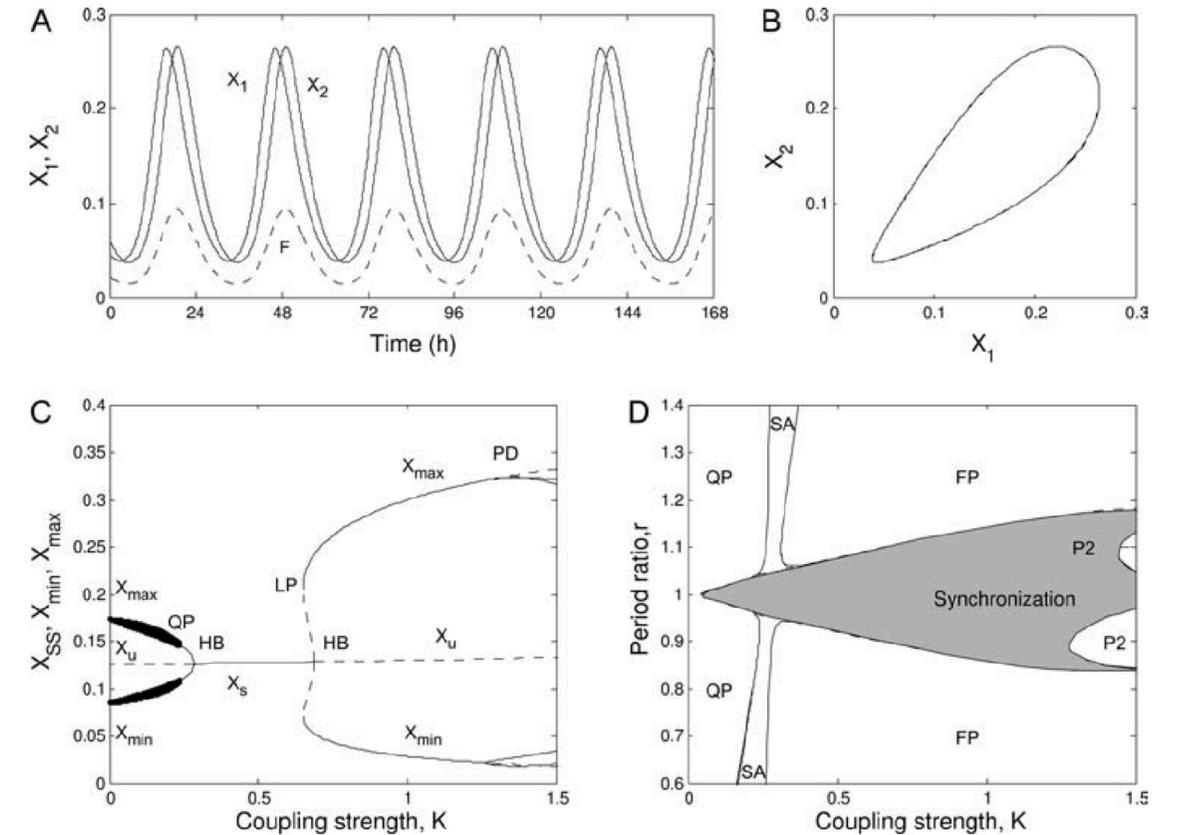
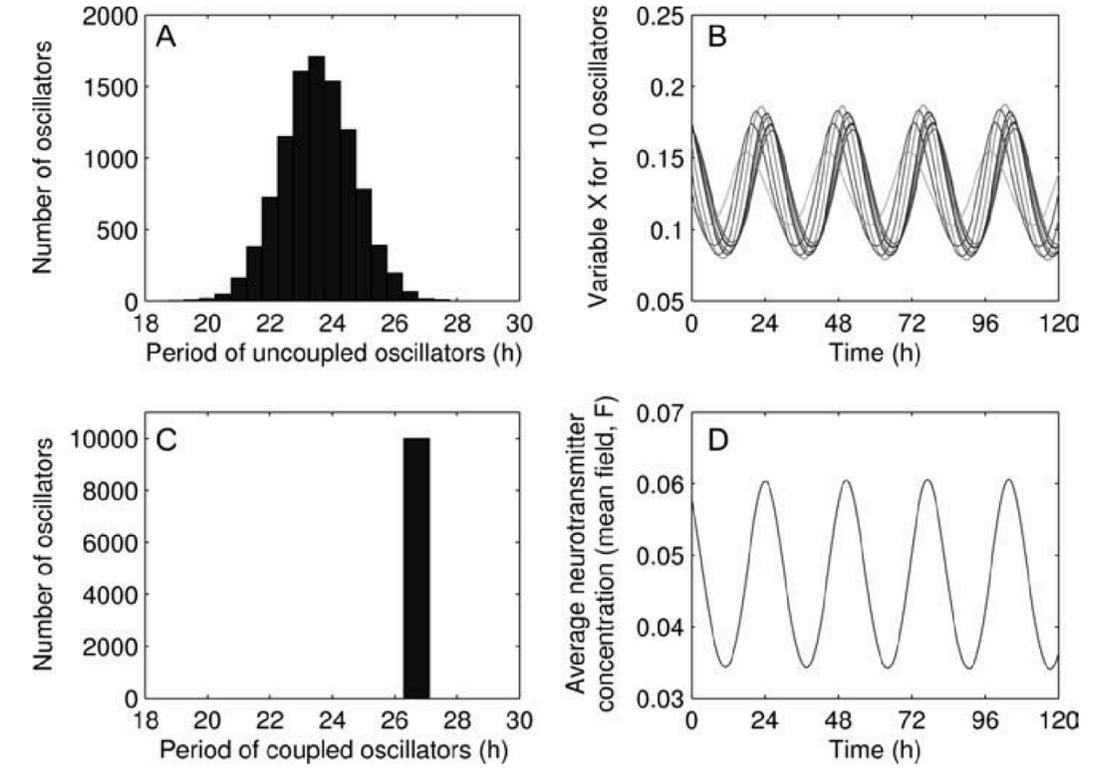
^{*}Institute for Theoretical Biology, Humboldt Universität zu Berlin, Berlin, Germany; [†]Unité de Chronobiologie Théorique, Université Libre de Bruxelles, Brussels, Belgium; and [‡]Laboratory of Chronobiology, Institute of Medical Immunology, Charité-Universitätsmedizin Berlin, Berlin, Germany

$$\frac{dX_i}{dt} = v_1 \frac{K_1^n}{K_1^n + Z_i^n} - v_2 \frac{X_i}{K_2 + X_i} + v_c \frac{KF}{K_c + KF} + L, \quad (1)$$

$$\frac{dY_i}{dt} = k_3 X_i - v_4 \frac{Y_i}{K_4 + Y_i}, \quad (2)$$

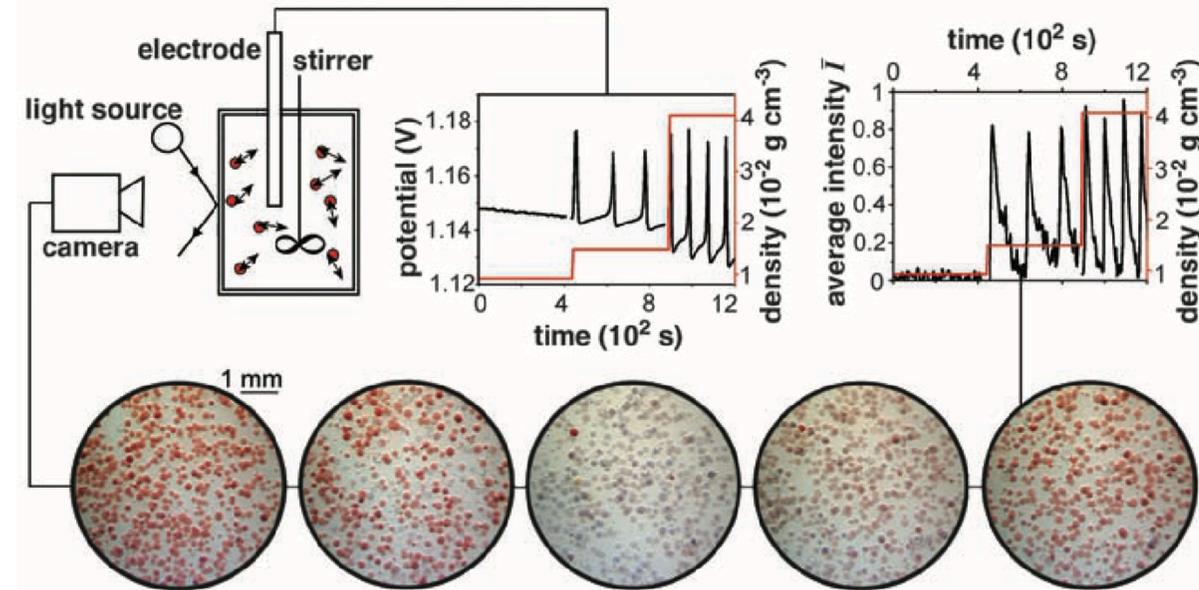
$$\frac{dZ_i}{dt} = k_5 Y_i - v_6 \frac{Z_i}{K_6 + Z_i}. \quad (3)$$

$$\frac{dV_i}{dt} = k_7 X_i - v_8 \frac{V_i}{K_8 + V_i}. \quad (4)$$



Dynamical Quorum Sensing and Synchronization in Large Populations of Chemical Oscillators

Annette F. Taylor,¹ Mark R. Tinsley,² Fang Wang,² Zhaoyang Huang,² Kenneth Showalter^{2*}



$$\frac{dX_i}{dt} = -k_{\text{ex}}(X_i - X_s) + f(X_i, Y_i, Z_i) \quad (1)$$

$$\frac{dX_s}{dt} = \frac{\bar{V}}{V_s} \sum_i N k_{\text{ex}}(X_i - X_s) + g(X_s, Y_s)$$

