

Cosmology from TGFT models of quantum gravity: basic ideas, relational observables and effective cosmological dynamics

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$a, b, c \in (1 \dots \infty) \sim \text{momenta on } T^3 = (S^1)^3$

UV cutoff N

$$S = \sum_{a,b,c} (\phi_{abc}(a^2 + b^2 + c^2)\phi_{abc} + \text{invariants})$$

non-local arguments which are dynamical,
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here: TGFT models for QG with quantum geometric data: GFT

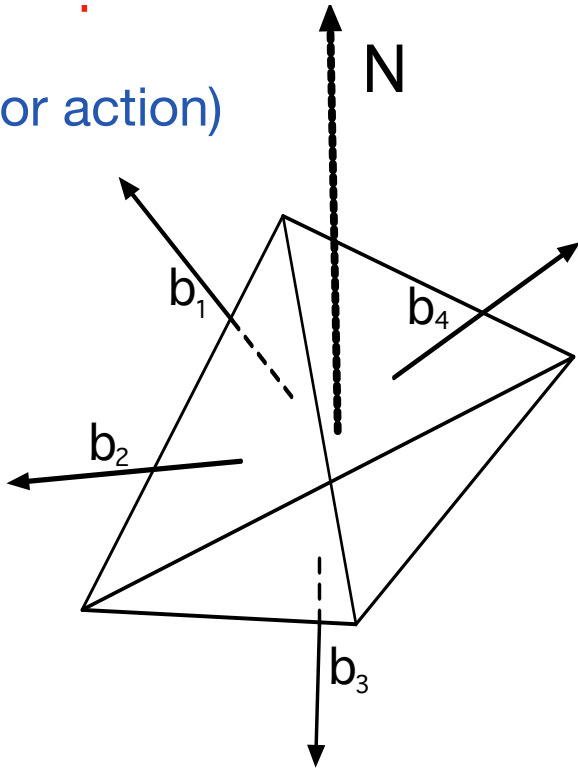
GFTs:
quantum geometric TGFT models

GFT (or "quantum geometric TGFT") models

4d case (rank d = 4)

tensor field on group manifold, endowed with "quantum geometric" conditions (in field or action)

$$\varphi : G^{\times d} \rightarrow \mathbb{C}$$



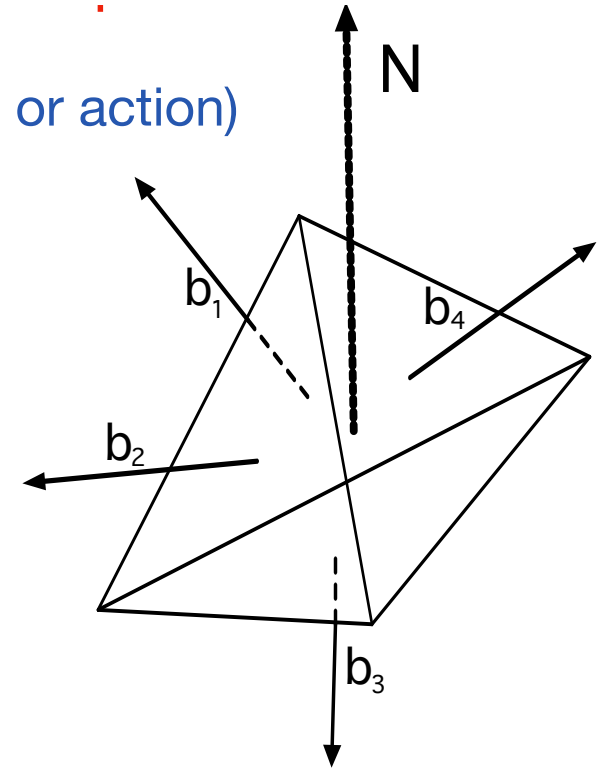
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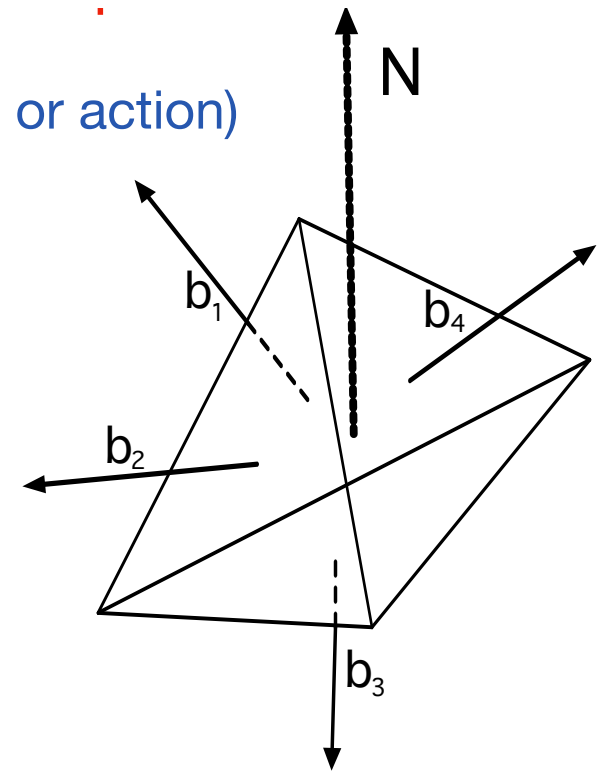
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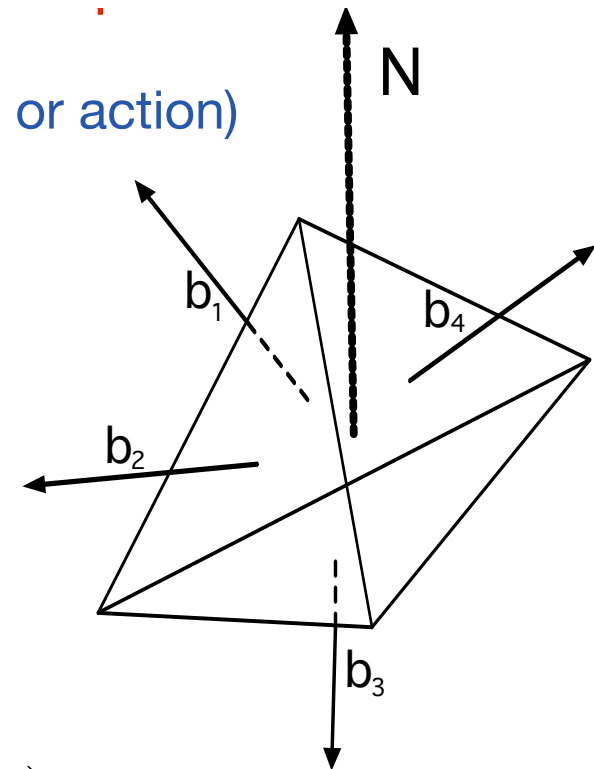
(quantum) geometric conditions on TGFT quanta (tetrahedra):

$$A_i n_i^I = b_i^I \in \mathbb{R}^{3,1} \quad b_i \cdot N = 0 \quad \sum_i b_i = 0 \quad b_i \in \mathbb{R}^3 \simeq \mathfrak{su}(2)$$

or equivalently:

$$(B_i^{IJ} \in \wedge^2 \mathbb{R}^{3,1} \simeq \mathfrak{so}(3,1), N^I \in \mathcal{T}\mathbb{R}^{3,1}) \quad N_I (*B_i^{IJ}) = 0 \quad \sum_i B_i^{IJ} = 0$$

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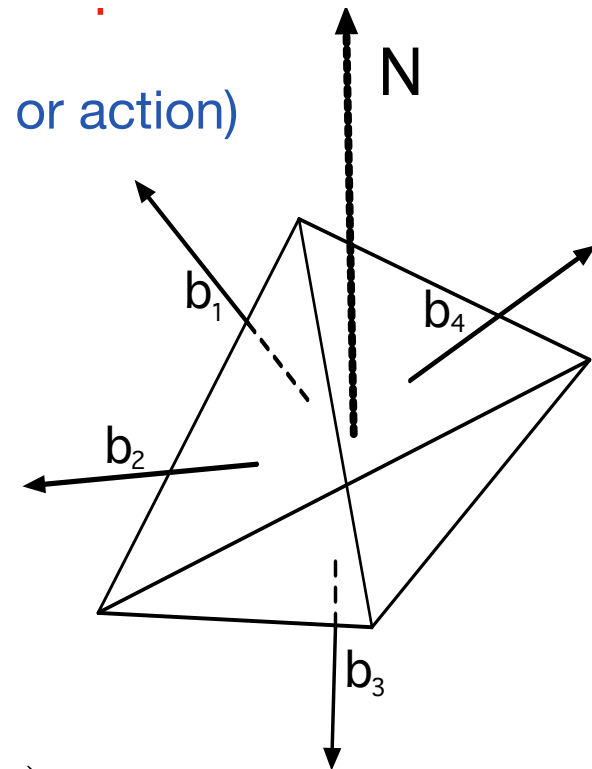
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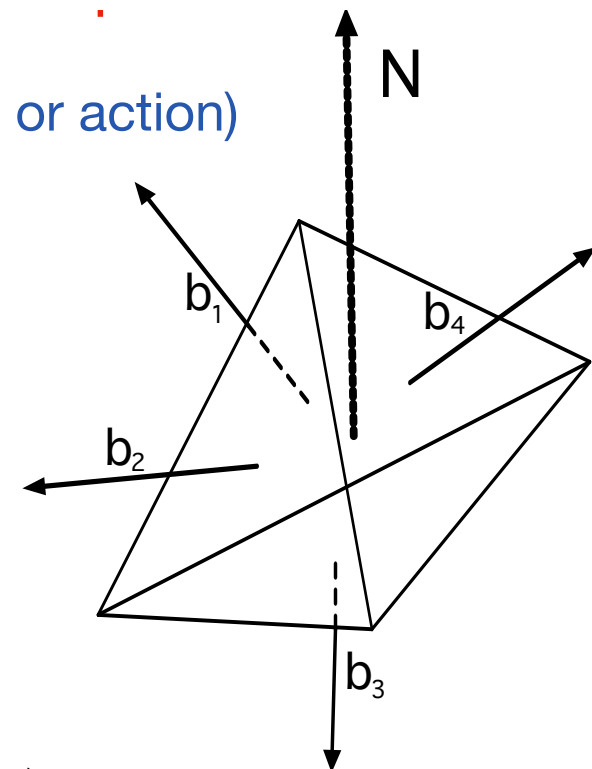
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phase space:

+ constraints

$$(\mathcal{T}^* SO(3,1))^4 \simeq (\mathfrak{so}(3,1) \times SO(3,1))^4 \supset (\mathfrak{so}(3) \times SO(3))^4 \simeq (\mathcal{T}^* SO(3))^4$$



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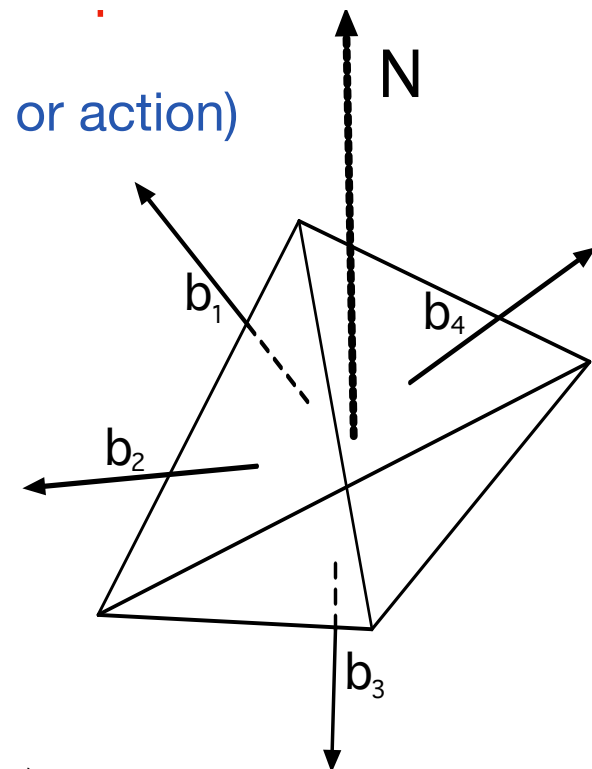
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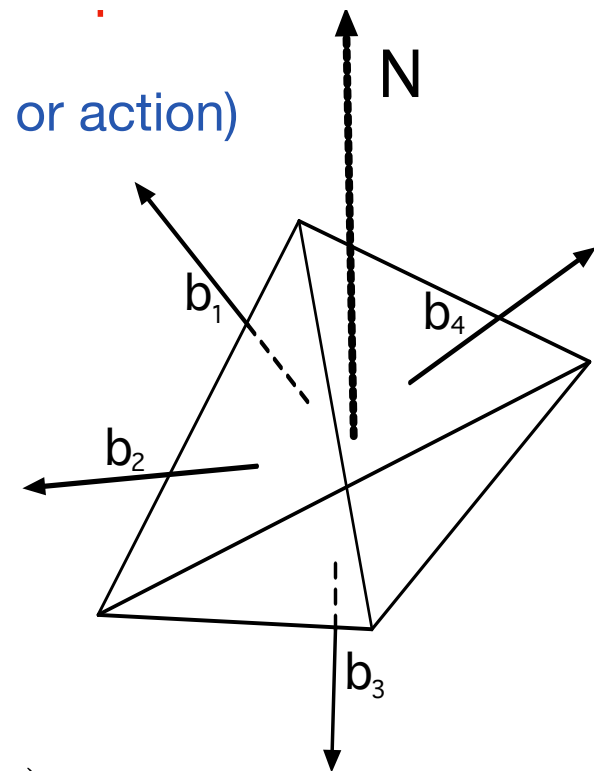
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• one can show that the two sets of data, with corresponding constraints, define same geometry

• indeed, one has (on solutions of the constraints): $B_i^{IJ} = N^I \wedge b_i^J$ "simple bivectors"

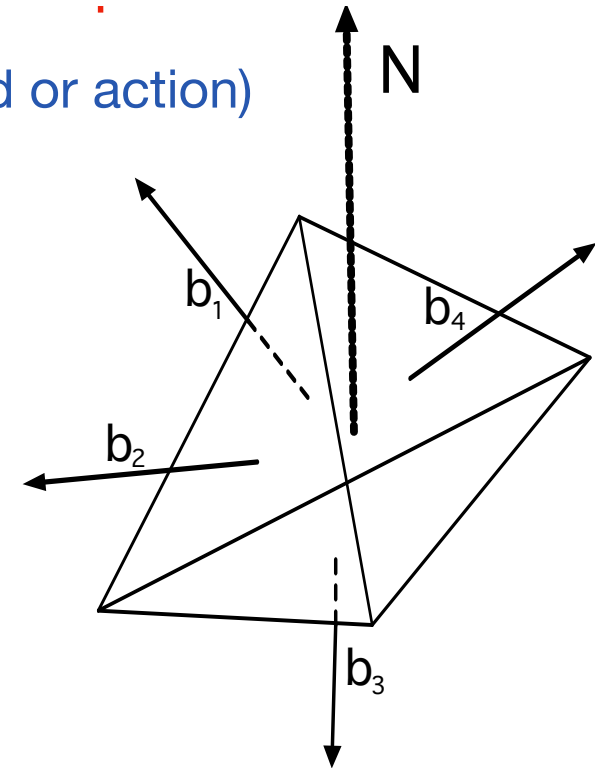


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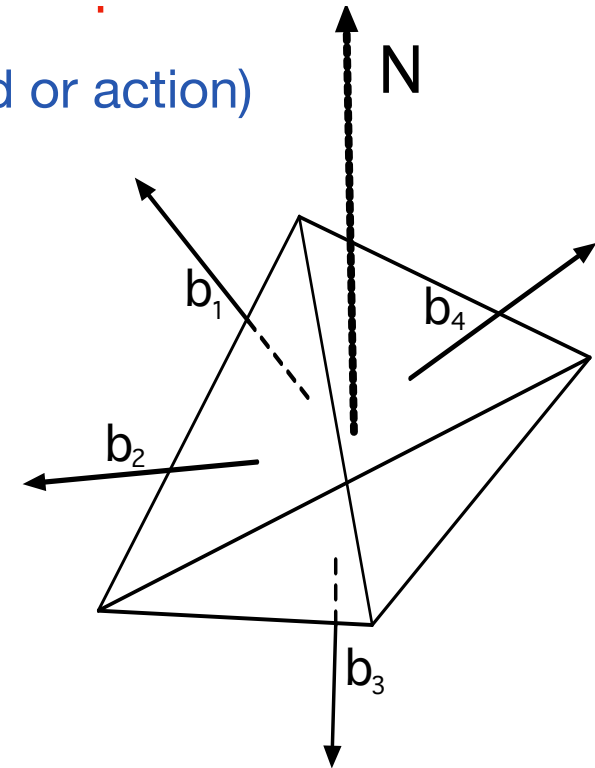
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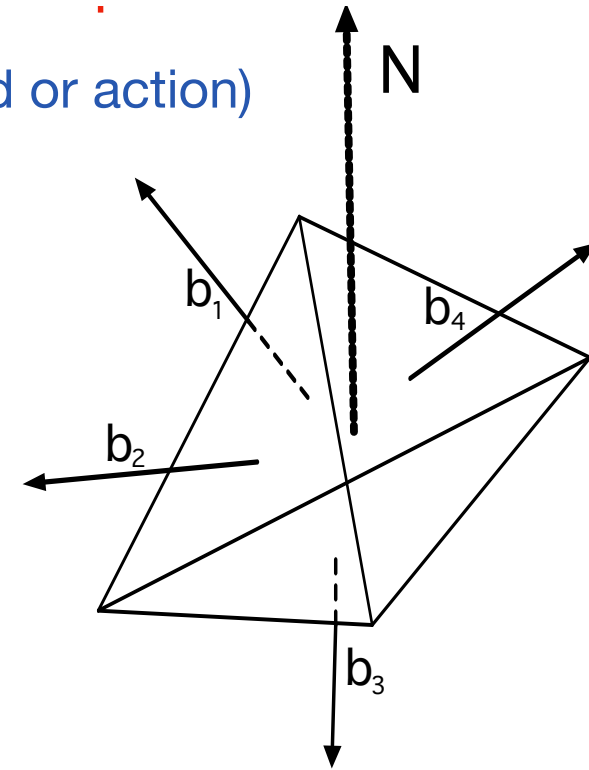
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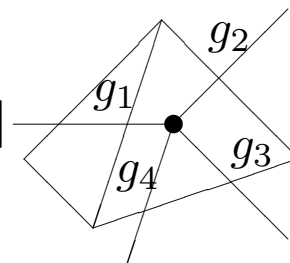
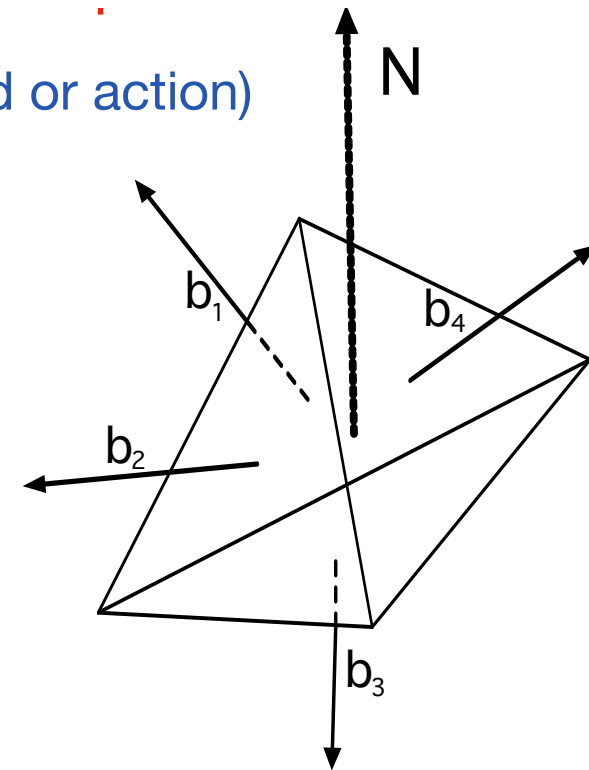
$$\hat{\varphi}^\dagger(g_1, g_2, g_3, g_4)|\emptyset\rangle = \left| \begin{array}{c} g_1 \\ g_2 \\ g_3 \\ g_4 \end{array} \right\rangle$$

Fock space of quantum states

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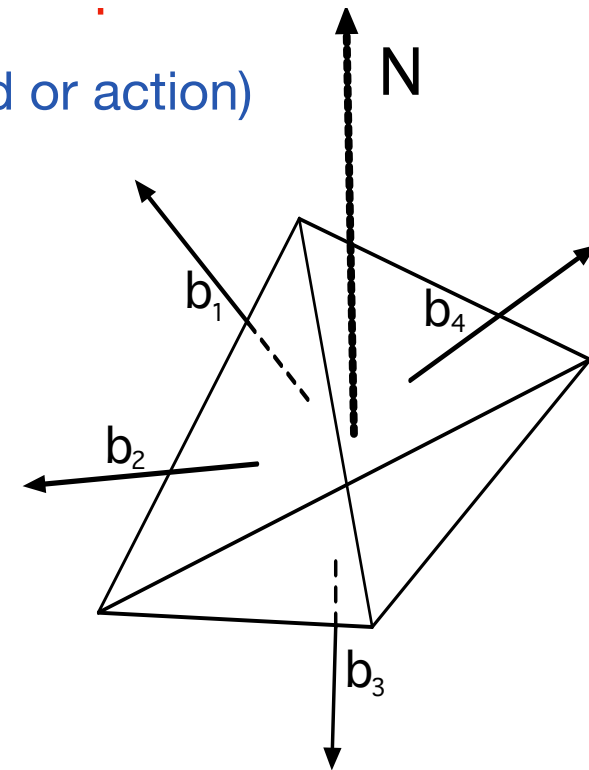
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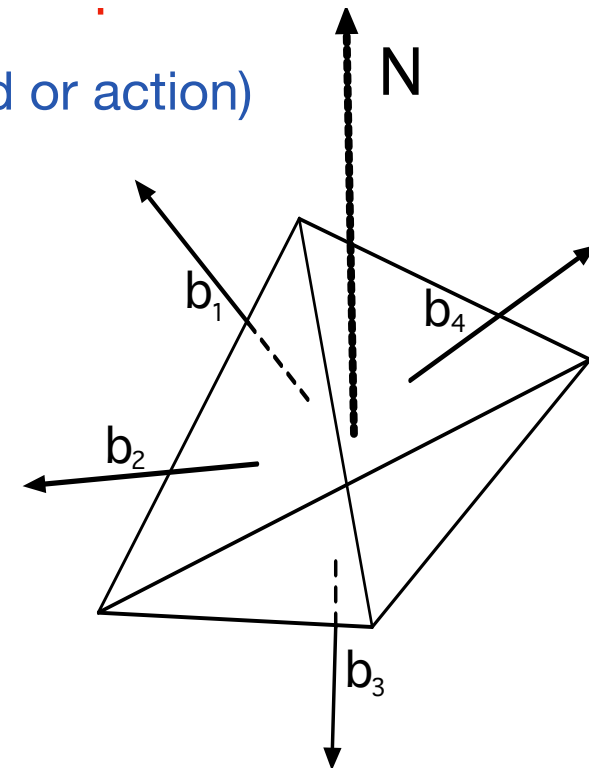
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$$S(\varphi, \bar{\varphi}) = \frac{1}{2} \int [dg_i] \overline{\varphi(g_i)} \mathcal{K}(g_i) \varphi(g_i) + \frac{\lambda}{D!} \int [dg_{ia}] \varphi(g_{i1}) \dots \varphi(\bar{g}_{iD}) \mathcal{V}(g_{ia}, \bar{g}_{iD}) + c.c.$$

$$\mathcal{Z} = \int \mathcal{D}\varphi \mathcal{D}\bar{\varphi} e^{i S_\lambda(\varphi, \bar{\varphi})} = \sum_{\Gamma} \frac{\lambda^{N_\Gamma}}{\text{sym}(\Gamma)} \mathcal{A}_\Gamma$$

non-local combinatorial pattern

perturbative expansion gives sum over simplicial complexes

perturbative amplitudes = simplicial gravity path integrals with dynamical discrete geometry (edge lengths,...)

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EPRL model

$$S = \sum_{\substack{j_{v_{ai}} \\ m_{v_{ai}}, \iota_a}} \bar{\varphi}_{m_{v_1}}^{j_{v_1} \iota_1} \varphi_{m_2}^{j_{v_2} \iota_2} (\mathcal{K}_2)^{j_{v_1} j_{v_2} \iota_1 \iota_2}_{m_{v_1}, m_{v_2}} + V$$

$$V = \sum_{j_i, m_i, \iota_i} \left[\varphi_{m_1 m_2 m_3 m_4}^{j_1 j_2 j_3 j_4 \iota_1} \varphi_{m_4 m_5 m_6 m_7}^{j_4 j_5 j_6 j_7 \iota_2} \varphi_{m_7 m_3 m_8 m_9}^{j_7 j_3 j_8 j_9 \iota_3} \varphi_{m_9 m_6 m_2 m_{10}}^{j_9 j_6 j_2 j_{10} \iota_4} \varphi_{m_{10} m_8 m_5 m_1}^{j_{10} j_8 j_5 j_1 \iota_5} \times \tilde{\mathcal{V}}_5(j_1, \dots, j_{10}; \iota_1, \dots, \iota_5) \right]$$

$$\tilde{\mathcal{V}}_5(j_{ab}, i_a) = \sum_{n_a} \int d\rho_a (n_a^2 + \rho_a^2) \left(\bigotimes_a f_{n_a \rho_a}^{i_a}(j_{ab}) \right) 15j_{SL(2, \mathbb{C})}((2j_{ab}, 2j_{ab}\gamma); (n_a, \rho_a))$$

$$f_{n\rho}^i := i^{m_1 \dots m_4} \bar{C}_{(j_1, m_1) \dots (j_4, m_4)}^{n\rho} \quad \rho = \gamma n \quad n = 2j$$

SL(2,C) data mapped to SU(2) ones; almost SU(2) spin network states; Immirzi parameter

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$$\begin{aligned} \text{irreps of SL(2,C)} \quad & \left(\prod_{a=1}^{10} (-1)^{-j_a - m_a} \right) \{10\rho\}_{\text{BC}} \varphi_{j_1 m_1 j_2 m_2 j_3 m_3 j_4 m_4}^{\rho_1 \rho_2 \rho_3 \rho_4} \varphi_{j_4 - m_4 j_5 m_5 j_6 m_6 j_7 m_7}^{\rho_4 \rho_5 \rho_6 \rho_7} \\ & \varphi_{j_7 - m_7 j_3 - m_3 j_8 m_8 j_9 m_9}^{\rho_7 \rho_3 \rho_8 \rho_9} \varphi_{j_9 - m_9 j_6 - m_6 j_2 - m_2 j_{10} m_{10}}^{\rho_9 \rho_6 \rho_2 \rho_{10}} \varphi_{j_{10} - m_{10} j_8 - m_8 j_5 - m_5 j_1 - m_1}^{\rho_{10} \rho_8 \rho_5 \rho_1} + c.c \end{aligned}$$

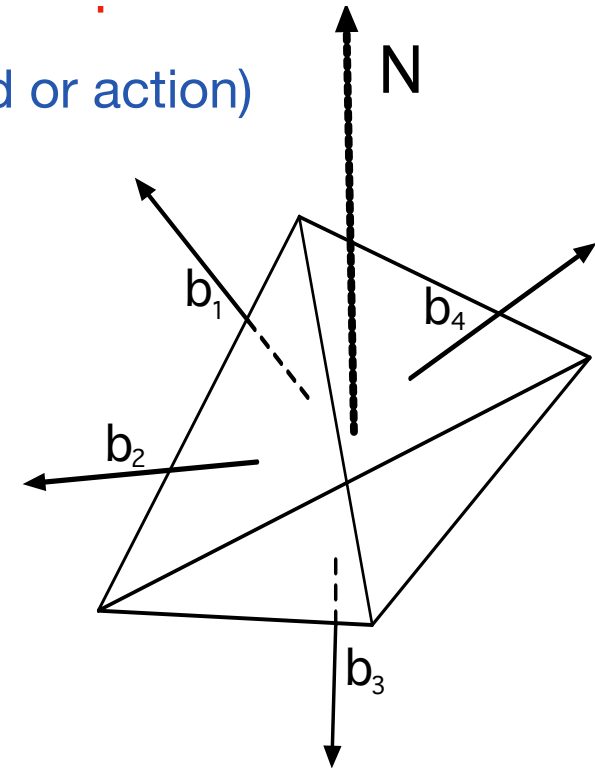
continuous SL(2,C) data; covariant "spin networks" states; no Immirzi parameter

GFT (or "quantum geometric TGFT") models

tensor field on group manifold, endowed with "quantum geometric" conditions (in field or action)

$$\varphi : G^{\times d} \rightarrow \mathbb{C}$$

TGFT quanta = geometric tetrahedra (group-theoretic data encode discrete geometry)



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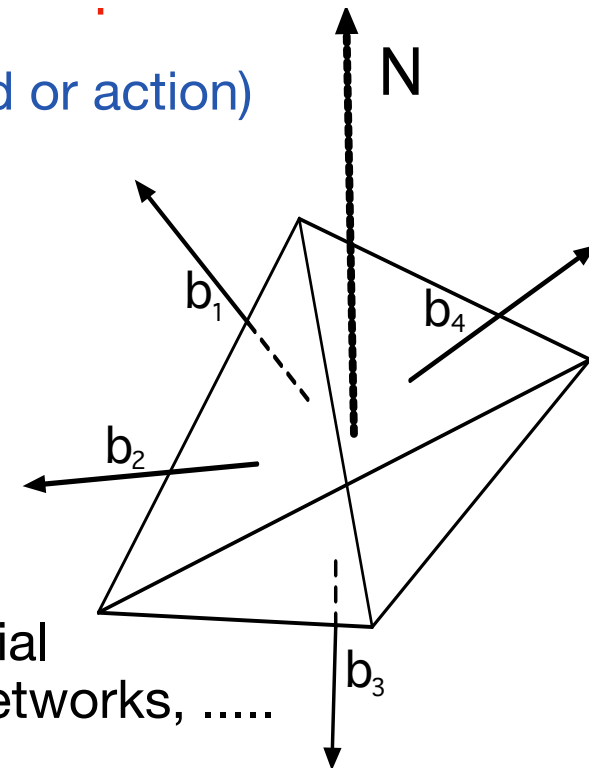
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- very rich quantum geometry (interplay of group& representation theory with simplicial geometry), full quantum many-body system (entanglement, ...), relation to tensor networks,
- close links with other QG formalisms:
 - quantum states are spin networks, 2nd quantized version of canonical LQG
 - Feynman amplitudes are spin foam amplitudes
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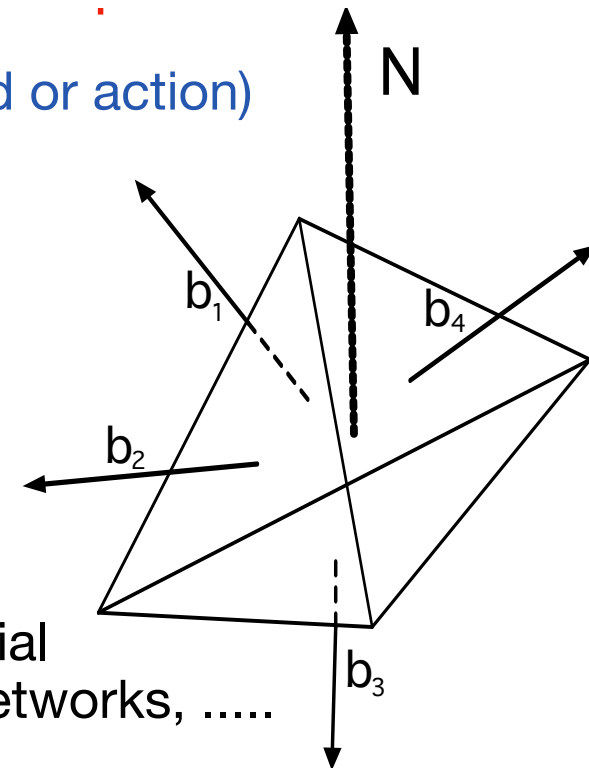
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- difficult to control quantum amplitudes, symmetries, etc
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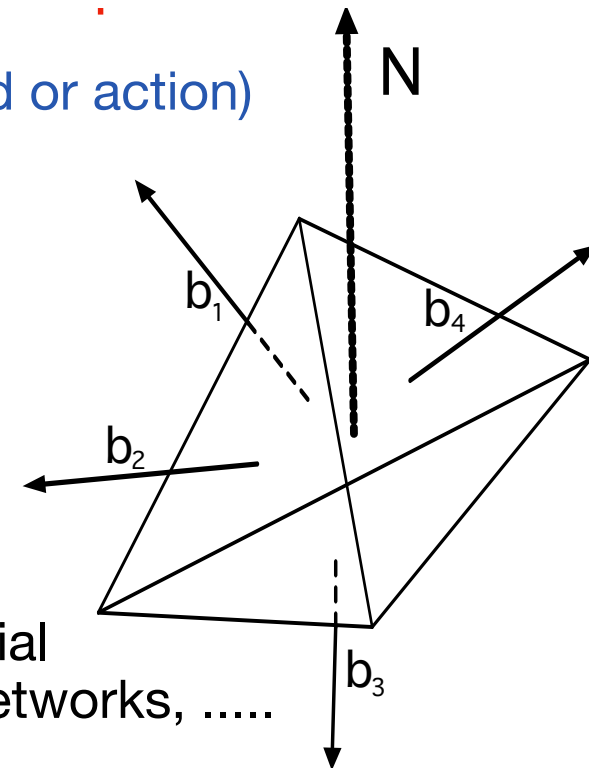


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why useful:

many geometric/physical guidelines and tools, and potentially meaningful even in simple approximations

see following

Adding matter to quantum geometry:
mixed local/non-local GFTs

Adding scalar matter to GFT

Y. Li, DO, M. Zhang, '17

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basic guideline for model-building (choosing GFT action):

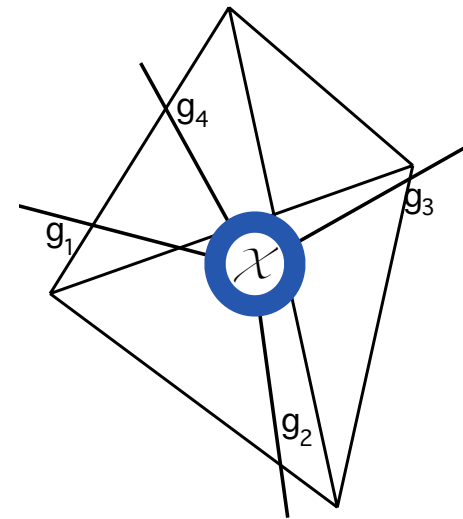
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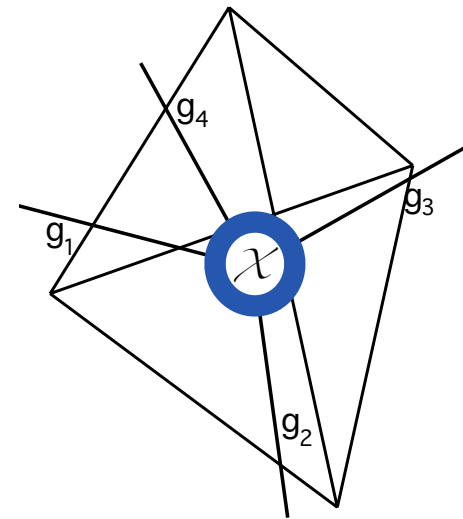
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- propagator (thus kinetic term) depends on difference between values at neighbouring 4-simplices
- domain of GFT field extended to include values of scalar fields $\hat{\varphi}(g_I, \chi^a) \equiv \hat{\varphi}(g_I, \chi^1, \dots, \chi^n)$

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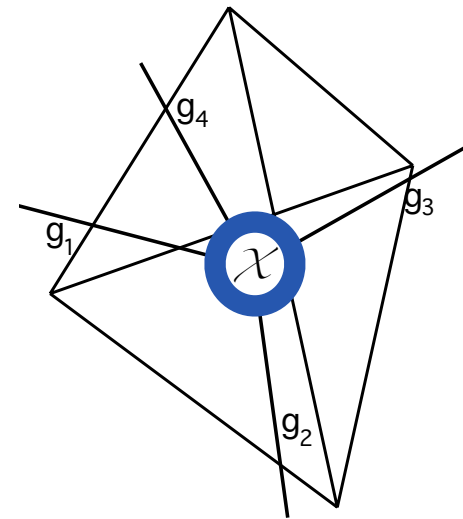
$$Z_{\phi G}^{\Delta} = \int \prod_{f \in \Delta} \mathcal{D}B_f \prod_{f \in \Delta^*} dg_{\ell} \prod_{v \in \Delta^*} d\phi_v \delta(S_{\gamma}(B_f)) e^{\frac{i}{\hbar}(S_{\phi}^{\Delta} + S_G^{\Delta})}$$

$$S_{\phi}^{\Delta} \equiv \left(\sum_{l \in \Delta^*} \tilde{V}_l \left(\frac{\delta_l \phi}{L_l} \right)^2 + \sum_{v \in \Delta^*} V_v \mathbb{V}(\phi_v) \right)$$

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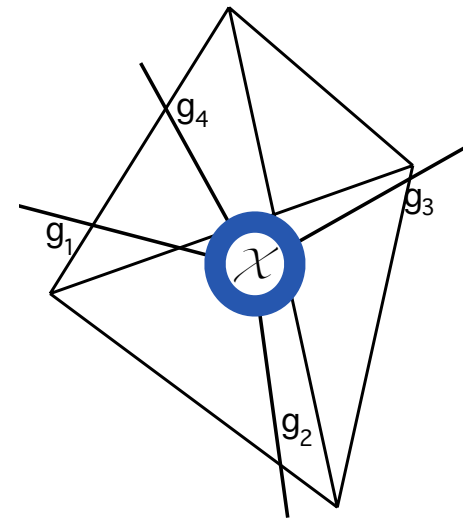
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- GFT propagator basically exponential of square of difference of scalar field values at neighbouring 4-simplices (coupled to discrete geometry), in discrete metric variables
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- GFT propagator basically exponential of square of difference of scalar field values at neighbouring 4-simplices (coupled to discrete geometry), in discrete metric variables
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- not unique: discretization + quantization ambiguities (only important to capture classical& continuum limit)

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example: extension to (real, massless, free, minimally coupled) scalar fields

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note: bringing together different branches of the TGFT family! (Y. Wang, V. Nador, DO, X. Pang, A. Tanasa, in progress)

Extracting continuum gravitational physics
from GFTs:
cosmology as QG hydrodynamics

Given GFT model, extract effective continuum gravitational physics

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$$F_\lambda(J) = \ln Z_\lambda[J] \quad \Gamma[\phi] = \sup_J (J \cdot \phi - F(J)) \quad \langle \varphi \rangle = \phi \quad \text{"mean field"}$$



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strategy:

- focus on quantum GFT effective action
- use the quantum geometric data of GFT (mean) field to gain physical intuition
- identify relevant geometric observables
- translate GFT (mean) field dynamics into dynamics for geometric observables



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corresponds to working with simplest condensate states
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isomorphism between domain of TGFT condensate wavefunction and minisuperspace

	$\sigma(\mathcal{D})$	\mathcal{D}	\simeq	$\{\text{geometries of tetrahedron}\} \simeq$
S. Gielen, '14			\simeq	$\{\text{continuum spatial geometries at a point}\} \simeq$
A. Jercher, DO, A. Pithis, '21			\simeq	minisuperspace of homogeneous geometries

+ homogeneous matter

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S. Gielen, '14		\simeq	$\{\text{continuum spatial geometries at a point}\}$	\simeq
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geometricity conditions
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BC model: $SL(2, \mathbb{C})^4 \longrightarrow \text{Hom}(2)^3$

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BC model:

$$\text{SL}(2, \mathbb{C})^4 \xrightarrow{\substack{\text{geometricity conditions} \\ \text{(simplicity + closure)}}} \text{Hom}(2)^3 \xrightarrow{\substack{\text{extra symmetry of} \\ \text{condensate wavefunction}}} \text{Hom}(2)^3 / \text{Ad}_{\text{SL}(2, \mathbb{C})}$$

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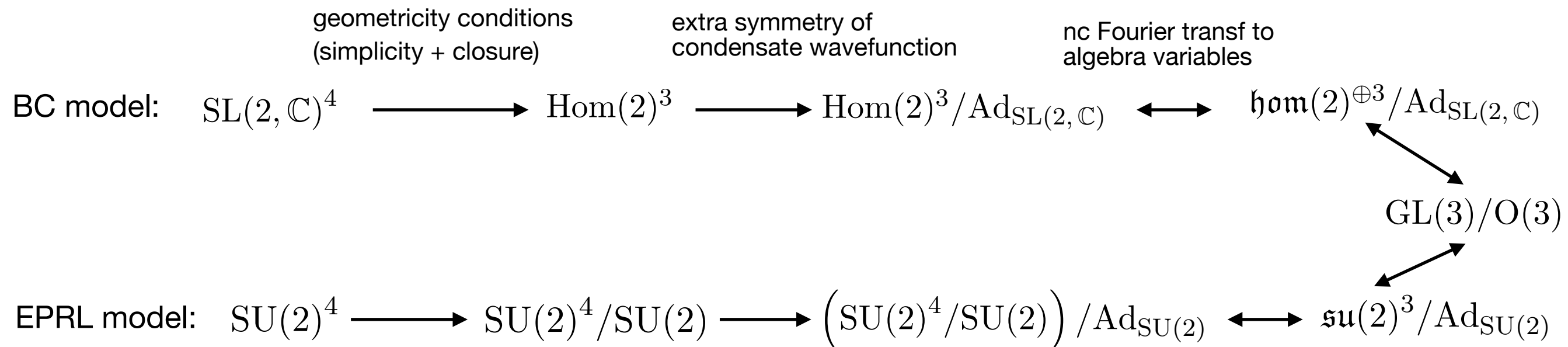
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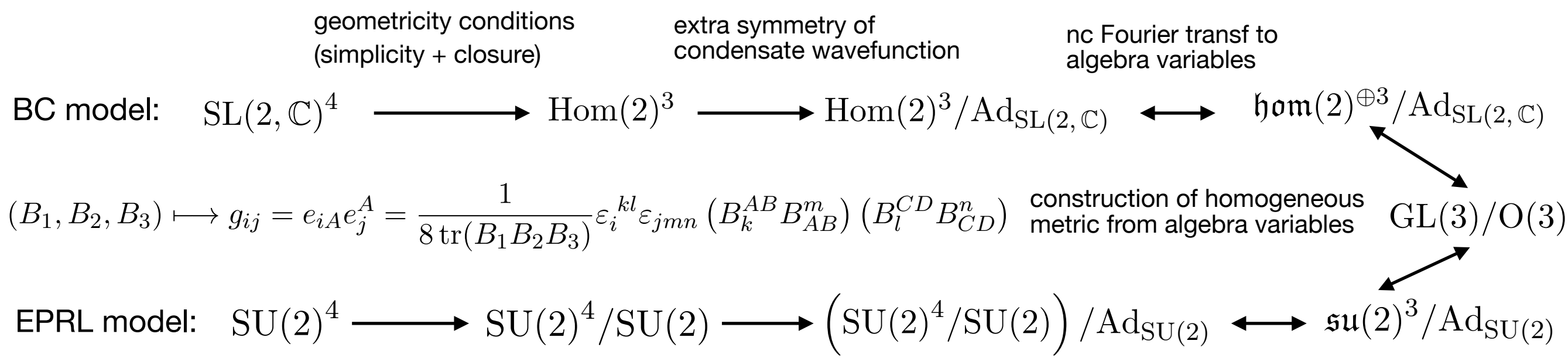
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Given GFT model, extract effective continuum gravitational physics

general: GFT hydro = non-linear quantum cosmology

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mean field hydrodynamic eqns = non-linear eqns for condensate wavefunction

S. Gielen, DO, L. Sindoni, '13

$$\int dh_I d\tilde{\chi} d\tilde{\phi} \mathcal{K} \left(g_I, h_I; \chi^\mu, \tilde{\chi}^\mu; \phi, \tilde{\phi} \right) \sigma(h_I, \tilde{\chi}^\mu, \tilde{\phi}) + \frac{\delta U(\varphi, \overline{\varphi})}{\delta \varphi(g_I, \chi^\mu, \phi)} \Big|_{\varphi \equiv \sigma} = 0$$

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mean field approx. corresponds to working with simplest condensate states (field coherent states):

mean field = condensate wavefunction

S. Gielen, DO, L. Sindoni, '13

$$|\sigma\rangle = \mathcal{N}_\sigma \exp \left[\int d^n \chi \int dg_I \sigma(g_I, \chi^a) \hat{\varphi}^\dagger(g_I, \chi^a) \right] |0\rangle$$

infinite superposition of quantum tetrahedra

Digression:
observables in QG and the relational strategy

Observables in (classical and quantum) General Relativity

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Spacetime is a physical system

gravitational field is metric field (gravity = spacetime geometry) - it is fully dynamical

Observables in (classical and quantum) General Relativity

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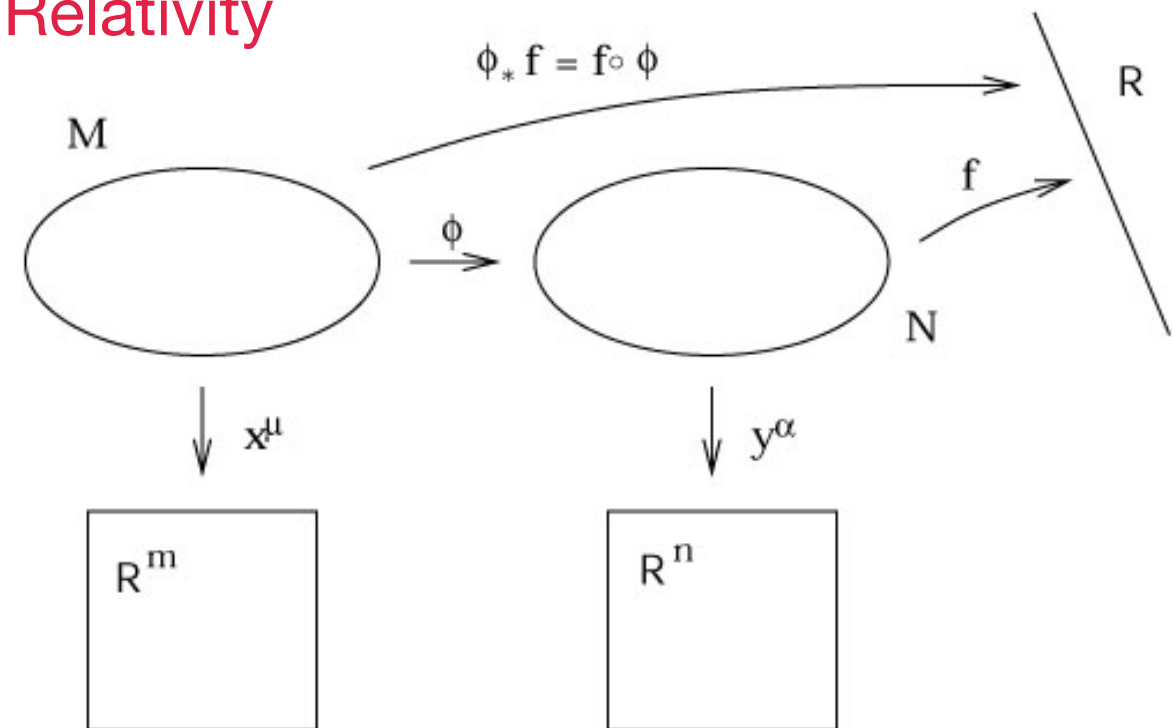
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general covariance (diffeo invariance):

no preferred local direction (or foliation)

no meaning of coordinates

no meaning of manifold points



Observables in (classical and quantum) General Relativity

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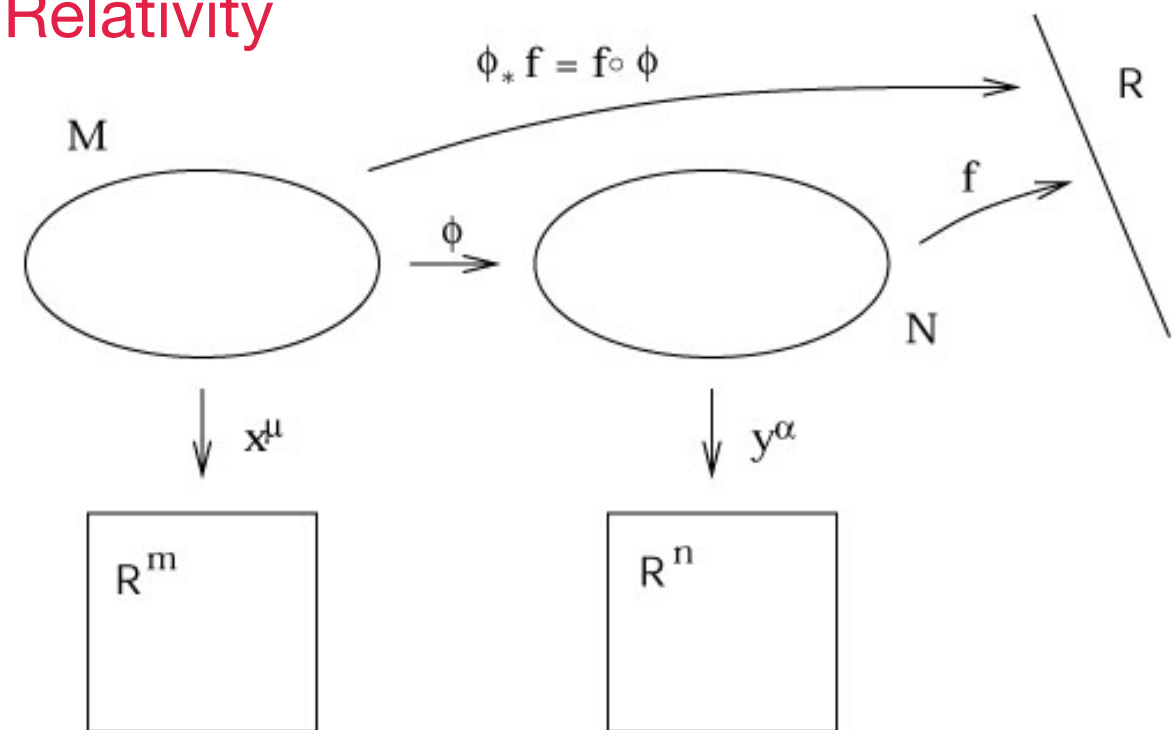
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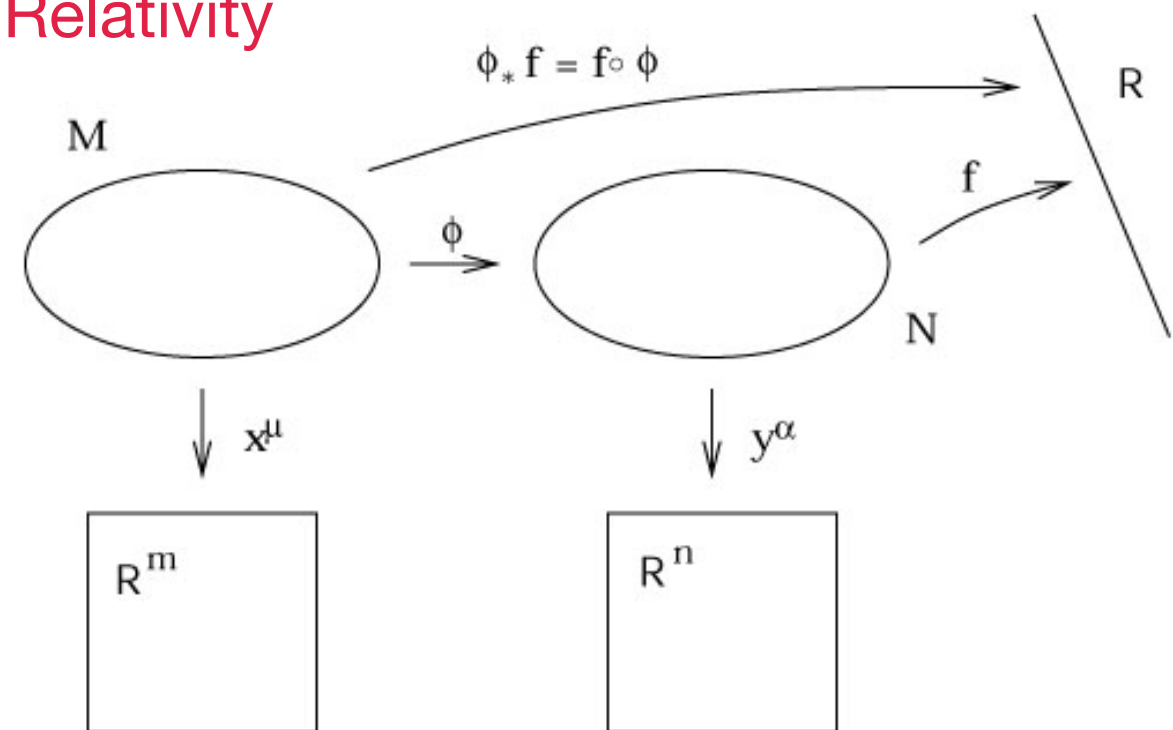
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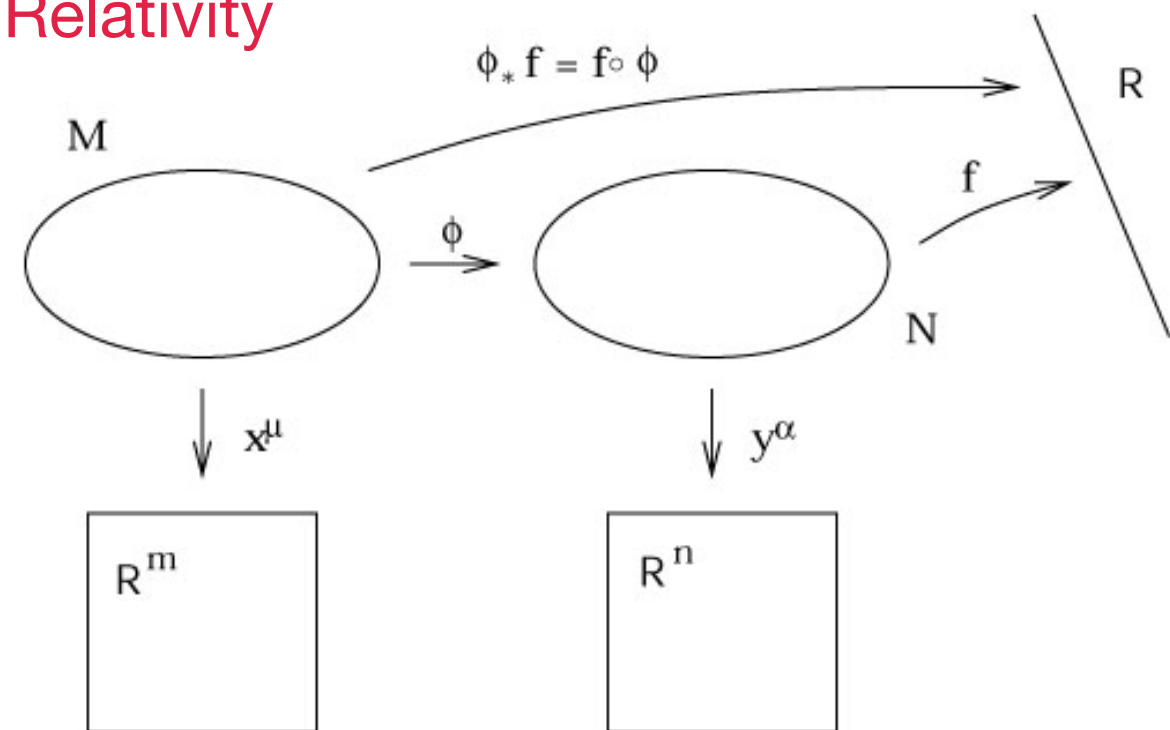
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- identify internal degrees of freedom of system, e.g. matter fields, and use them as (approximate) clocks and rods to parametrize the evolution and location of other degrees of freedom



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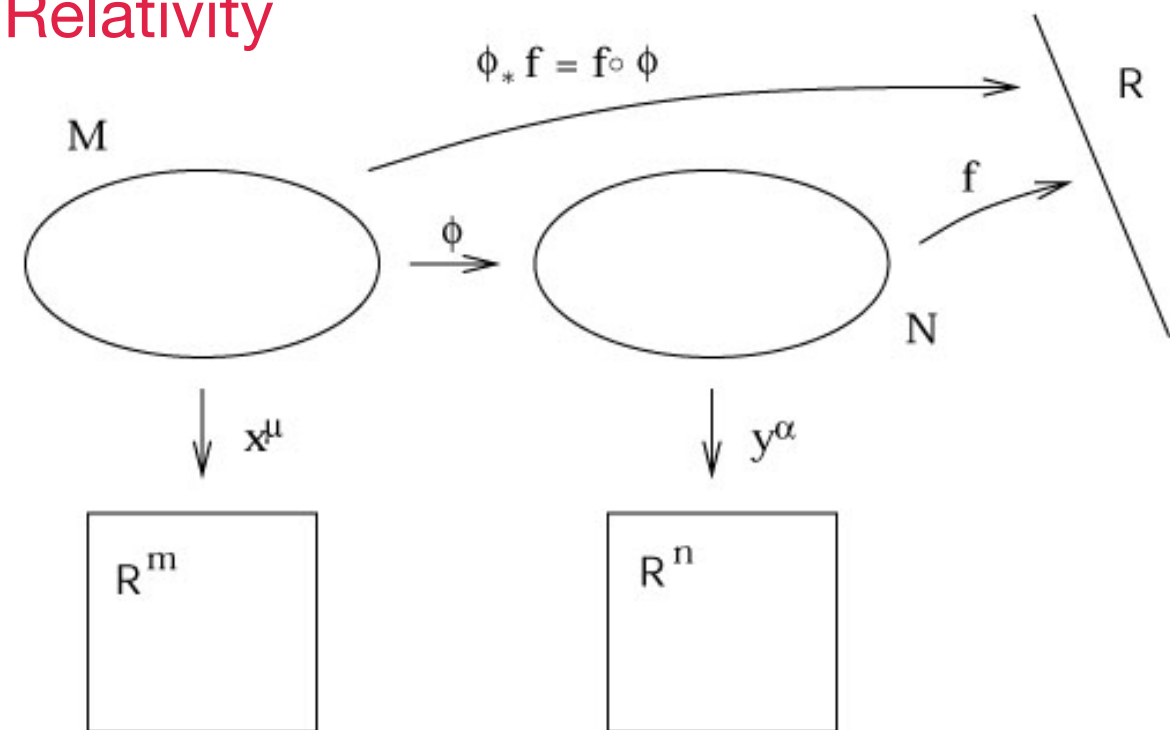
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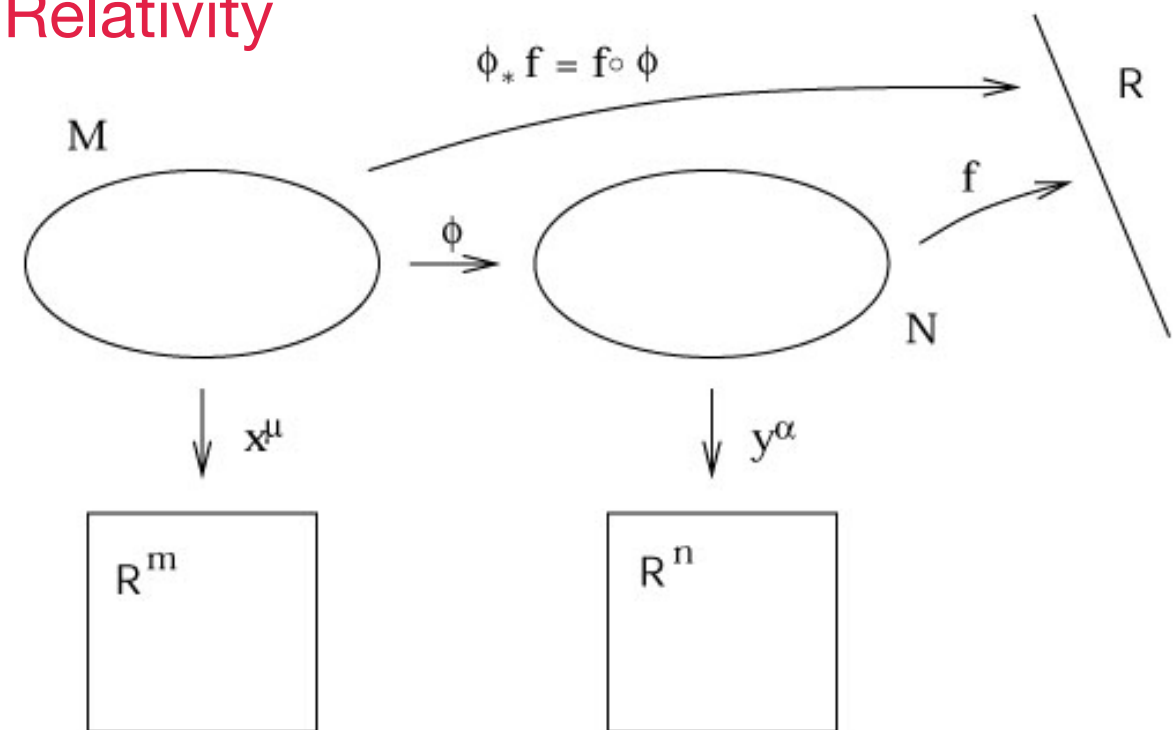
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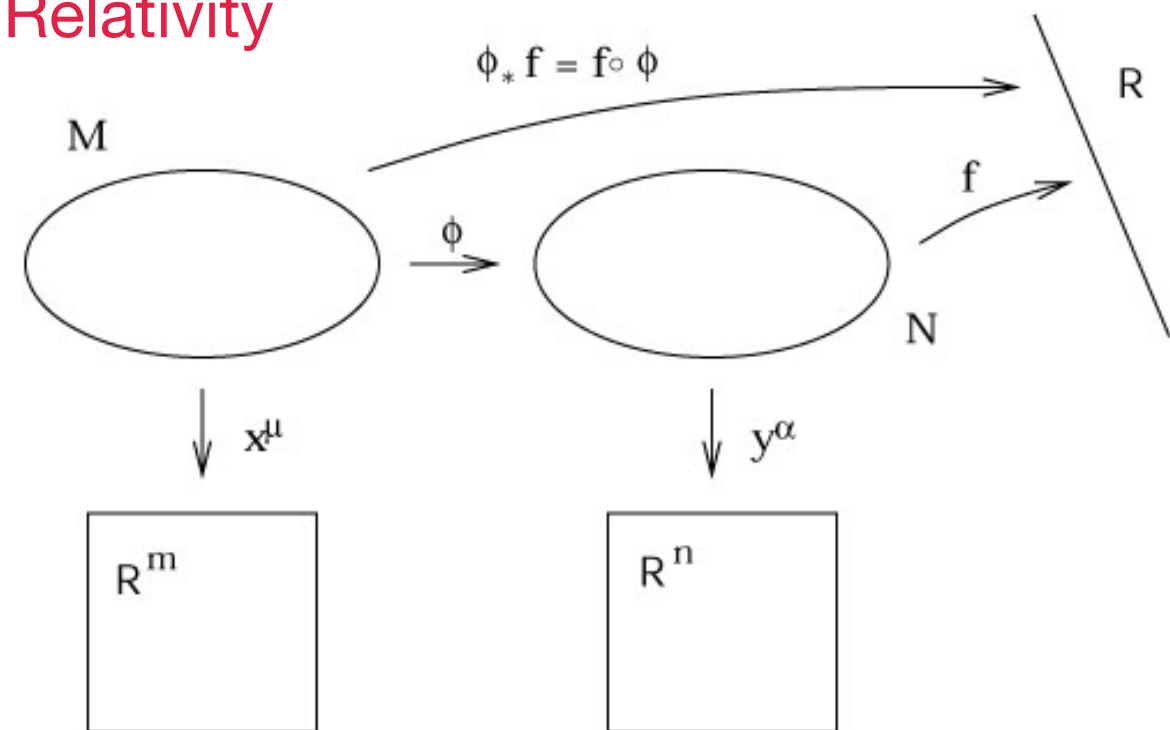
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manifold could in principle disappear from relevant physical description



Extracting continuum gravitational physics from GFTs: GFT condensate cosmology

GFT condensate cosmology: general hydrodynamic equations

GFT condensate cosmology (for EPRL and BC models)

general form of GFT action for QG coupled to (five) massless free scalar fields

$$\begin{aligned} S(\varphi, \bar{\varphi}) &= K + U \\ K &= \int dg_I dh_I \int d^d\chi d^d\chi' d\phi d\phi' \bar{\varphi}(g_I, \chi) \mathcal{K}(g_I, h_I; (\chi - \chi')_\lambda^2, (\phi - \phi')^2) \varphi(h_I, (\chi')^\mu, \phi') \\ U &= \int d^d\chi d\phi \int \left(\prod_{a=1}^5 dg_I^a \right) \mathcal{U}(g_I^1, \dots, g_I^5) \prod_{\ell=1}^5 \varphi(g_I^\ell, \chi^\mu, \phi) + \text{c.c.} \\ &\quad (\chi - \chi')_\lambda^2 \equiv \text{sgn}(\lambda) M_{\mu\nu}^{(\lambda)} (\chi - \chi')^\mu (\chi - \chi')^\nu \end{aligned}$$

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hydrodynamics in mean field approx. for special "good clock+rods" states

S. Gielen, DO, L. Sindoni, '13

$$\begin{aligned}
 \left\langle \frac{\delta S_{\text{GFT}}[\hat{\varphi}, \hat{\varphi}^\dagger]}{\delta \hat{\varphi}^\dagger(g_I, \chi_0)} \right\rangle_{\sigma_{\epsilon^\mu}; x^\mu, \pi_\mu} &\equiv \left\langle \sigma_{\epsilon^\mu}; x^\mu, \pi_\mu \left| \frac{\delta S_{\text{GFT}}[\hat{\varphi}, \hat{\varphi}^\dagger]}{\delta \hat{\varphi}^\dagger(g_I, \chi_0)} \right| \sigma_{\epsilon^\mu}; x^\mu, \pi_\mu \right\rangle = 0 \\
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restriction to "good clock+rods" simple condensate states

$$\sigma_{\epsilon, \delta, \pi_0, \pi_x; x^\mu}(g_I, \chi^\mu, \phi) = \eta_\epsilon(\chi^0 - x^0; \pi_0) \eta_\delta(|\chi - \mathbf{x}|; \pi_x) \tilde{\sigma}(g_I, \chi^\mu, \phi)$$

L. Marchetti, DO, '20, '21

$$|\chi - \mathbf{x}|^2 = \sum_{i=1}^d (\chi^i - x^i)^2 \quad \mathbb{C} \ni \delta = \delta_r + i\delta_i \quad \delta_r > 0 \quad \epsilon, |\delta| \ll 1 \quad z_0 \equiv \epsilon \pi_0^2 / 2 \quad z \equiv \delta \pi_x^2 / 2$$

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this turns non-linear quantum cosmology eqn into a relational evolution eqn for condensate wavefunction
in terms of relational "time" and "space" directions, defined by physical frame

we analyse it first under two simplifying assumptions:

- subdominant GFT interactions: $U \ll K$; consistent with spin foam and discrete gravity interpretation

- **isotropy:**
$$\sigma(g_I, \chi^a) = \sum_{j=0}^{\infty} \sigma_j(\chi^a) \mathcal{I}_{m_1 m_2 m_3 m_4}^{*jjjj, \iota_+} \mathcal{I}_{n_1 n_2 n_3 n_4}^{jjjj, \iota_+} \sqrt{d(j)^4} \prod_{i=1}^4 D_{m_i n_i}^j(g_I) \quad d(j) = 2j + 1$$

largest eigenvalue of volume
compatible with j



condensate wavefunction depends on single j

note: adopt notation for EPRL SU(2)-based model, but analysis and results apply equally to BC model

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resulting mean field hydrodynamics eqn:

$$\partial_0^2 \tilde{\sigma}_j(x, \pi_\phi) - i\gamma \partial_0 \tilde{\sigma}_j(x, \pi_\phi) - {}^{(\lambda)}E_j^2(\pi_\phi) \tilde{\sigma}_j(x, \pi_\phi) + \alpha^2 \nabla^2 \tilde{\sigma}_j(x, \pi_\phi) = 0$$

Fourier mode of matter field variable

$$\gamma \equiv \frac{\sqrt{2\epsilon} z_0}{\epsilon z_0^2} \quad {}^{(\lambda)}E_j^2 \equiv \frac{1}{\epsilon z_0^2} - r_{j;2}(\pi_\phi) (1 + 3\lambda\alpha^2) \quad \alpha^2 \equiv \frac{1}{3} \frac{\delta z^2}{\epsilon z_0^2} \quad r_s^{(\lambda)} \equiv \frac{\tilde{K}_\lambda^{(s)}}{\tilde{K}_\lambda^{(0)}}$$

dependence on both GFT model and states

linear part of non-linear hydro eqns

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Fourier mode of matter field variable

dependence on both GFT model and states

linear part of non-linear hydro eqns

using: $\tilde{\sigma}_j \equiv \rho_j \exp[i\theta_j]$

rewrite in standard hydrodynamic form (fluid density, phase)

we analyse it first under two simplifying assumptions:

- subdominant GFT interactions: $U \ll K$; consistent with spin foam and discrete gravity interpretation

- **isotropy:**
$$\sigma(g_I, \chi^a) = \sum_{j=0}^{\infty} \sigma_j(\chi^a) \mathcal{I}_{m_1 m_2 m_3 m_4}^{*jjjj, \iota_+} \mathcal{I}_{n_1 n_2 n_3 n_4}^{jjjj, \iota_+} \sqrt{d(j)^4} \prod_{i=1}^4 D_{m_i n_i}^j(g_I) \quad d(j) = 2j + 1$$

largest eigenvalue of volume compatible with j

condensate wavefunction depends on single j

note: adopt notation for EPRL SU(2)-based model, but analysis and results apply equally to BC model

resulting mean field hydrodynamics eqn:

$$\partial_0^2 \tilde{\sigma}_j(x, \pi_\phi) - i\gamma \partial_0 \tilde{\sigma}_j(x, \pi_\phi) - {}^{(\lambda)}E_j^2(\pi_\phi) \tilde{\sigma}_j(x, \pi_\phi) + \alpha^2 \nabla^2 \tilde{\sigma}_j(x, \pi_\phi) = 0$$

Fourier mode of matter field variable

$$\gamma \equiv \frac{\sqrt{2\epsilon} z_0}{\epsilon z_0^2} \quad {}^{(\lambda)}E_j^2 \equiv \frac{1}{\epsilon z_0^2} - r_{j;2}(\pi_\phi) (1 + 3\lambda \alpha^2) \quad \alpha^2 \equiv \frac{1}{3} \frac{\delta z^2}{\epsilon z_0^2} \quad r_s^{(\lambda)} \equiv \frac{\tilde{K}_\lambda^{(s)}}{\tilde{K}_\lambda^{(0)}}$$

dependence on both GFT model and states

linear part of non-linear hydro eqns

using: $\tilde{\sigma}_j \equiv \rho_j \exp[i\theta_j]$

rewrite in standard hydrodynamic form (fluid density, phase)

$$0 = \rho_j'' + \text{Re } \alpha^2 \nabla^2 \rho_j - \left[(\theta_j')^2 + {}^{(\lambda)}\eta_j^2 - \gamma \theta_j' - \text{Re } \alpha^2 (\nabla \theta_j)^2 - \text{Im } \alpha^2 \nabla^2 \theta_j \right] \rho_j - 2 \nabla \rho_j \cdot \nabla \theta_j$$

$$0 = \theta_j'' \rho_j + 2\theta_j' \rho_j' - \gamma \rho_j' + \text{Re } \alpha^2 [2 \nabla \rho_j \cdot \nabla \theta_j + \nabla^2 \theta_j \rho_j] - {}^{(\lambda)}\beta_j^2 \rho_j + \text{Im } \alpha^2 [\nabla^2 \rho_j - (\nabla \theta_j)^2 \rho_j]$$

$${}^{(\lambda)}\eta_j^2 \equiv \frac{1}{\epsilon z_0^2} - r_{j;2}(\pi_\phi) (1 + 3\lambda \text{Re } \alpha^2) \quad {}^{(\lambda)}\beta_j^2 = 3\lambda \text{Im } \alpha^2 r_{j;2}$$

decomposition into homogeneous background + perturbations

L. Marchetti, DO, '21

decomposition into homogeneous background + perturbations

homogeneous background + inhomogeneous perturbations (defined in relational terms)

L. Marchetti, DO, '21

$$\rho_j = \bar{\rho}_j + \delta\rho_j \quad \theta_j \equiv \bar{\theta}_j + \delta\theta_j \quad \bar{\rho} = \bar{\rho}(x^0, \pi_\phi) \quad \bar{\theta} = \bar{\theta}(x^0, \pi_\phi)$$

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background eqns:

$$\bar{\rho}_j''(x^0, \pi_\phi) - \left[(\bar{\theta}_j'(x^0, \pi_\phi))^2 + {}^{(\lambda)}\eta_j^2(\pi_\phi) - \gamma \bar{\theta}_j'(x^0, \pi_\phi) \right] \bar{\rho}_j(x^0, \pi_\phi) = 0$$

$$\bar{\theta}_j''(x^0, \pi_\phi) + (\bar{\theta}_j'(x^0, \pi_\phi) - \gamma/2) \frac{(\bar{\rho}_j^2)'(x^0, \pi_\phi)}{\bar{\rho}_j^2(x^0, \pi_\phi)} - {}^{(\lambda)}\beta_j^2 = 0$$

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$$\text{assume } |\text{Im } \alpha^2| = \frac{2}{3} \frac{\pi_x^2 \delta_r |\delta_i|}{\epsilon^2 \pi_0^2} \ll 1 \quad \longrightarrow \quad {}^{(\lambda)}\beta_j^2 = 3\lambda \text{Im } \alpha^2 r_{j;2} \quad \text{negligible}$$

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Q_j, \mathcal{E}_j are integration constants (conserved quantities)

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perturbations eqns:

highly coupled; decouple for large condensate density (large universe volume) and $|\text{Im } \alpha^2| = \frac{2}{3} \frac{\pi_x^2 \delta_r |\delta_i|}{\epsilon^2 \pi_0^2} \ll 1$

$$0 \simeq \delta\rho_j''(x, \pi_\phi) - \nabla^2 \delta\rho_j(x, \pi_\phi) - {}^{(\lambda)}\eta_j^2(\pi_\phi) \delta\rho_j(x, \pi_\phi)$$

$$0 \simeq \delta\theta_j''(x, \pi_\phi) + 2\delta\theta_j'(x, \pi_\phi) \frac{\bar{\rho}_j'(x^0, \pi_\phi)}{\bar{\rho}_j(x^0, \pi_\phi)} - \nabla^2 \delta\theta_j(x, \pi_\phi)$$

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\longrightarrow

$$\bar{\theta}_j'(x^0, \pi_\phi) = \frac{\gamma}{2} + \frac{Q_j(\pi_\phi)}{\bar{\rho}_j^2(x^0, \pi_\phi)} \quad (\bar{\rho}_j^2)'(x^0, \pi_\phi) = \mathcal{E}_j(\pi_\phi) - \frac{Q_j^2(\pi_\phi)}{\bar{\rho}_j^2(x^0, \pi_\phi)} + \mu_j^2(\pi_\phi) \bar{\rho}_j^2(x^0, \pi_\phi)$$

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dependence on both GFT model and condensate states

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dependence on both GFT model and condensate states

now, need to obtain equations for physical observables

GFT condensate cosmology:
emergent dynamics of physical observables



used to define collective relational observables for effective continuum dynamics

as expectation values in "good clock+rods" condensate states

$$N(x^0, x^i) \equiv \langle \sigma_{\epsilon, \delta, \pi_0, \pi_x, x^\mu} | \hat{N} | \sigma_{\epsilon, \delta, \pi_0, \pi_x, x^\mu} \rangle$$

$$V(x^0, x^i) \equiv \langle \sigma_{\epsilon, \delta, \pi_0, \pi_x, x^\mu} | \hat{V} | \sigma_{\epsilon, \delta, \pi_0, \pi_x, x^\mu} \rangle$$

$$X^\mu(x^0, x^i) \equiv \langle \sigma_{\epsilon, \delta, \pi_0, \pi_x, x^\mu} | \hat{V} | \sigma_{\epsilon, \delta, \pi_0, \pi_x, x^\mu} \rangle \simeq x^\mu$$

$$\Pi(x^0, x^i) \equiv \langle \sigma_{\epsilon, \delta, \pi_0, \pi_x, x^\mu} | \hat{\Pi}_\nu | \sigma_{\epsilon, \delta, \pi_0, \pi_x, x^\mu} \rangle$$

$$\phi(x^0, x^i) \equiv \langle \sigma_{\epsilon, \delta, \pi_0, \pi_x, x^\mu} | \hat{\Phi} | \sigma_{\epsilon, \delta, \pi_0, \pi_x, x^\mu} \rangle$$

$$\Pi_\phi(x^0, x^i) \equiv \langle \sigma_{\epsilon, \delta, \pi_0, \pi_x, x^\mu} | \hat{\Pi}_\phi | \sigma_{\epsilon, \delta, \pi_0, \pi_x, x^\mu} \rangle$$

- number operator

$$\hat{N} = \int d^n \chi \int dg_I \hat{\varphi}^\dagger(g_I, \chi^a) \hat{\varphi}(g_I, \chi^a)$$

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$$V(x^0, x^i) \equiv \langle \sigma_{\epsilon, \delta, \pi_0, \pi_x, x^\mu} | \hat{V} | \sigma_{\epsilon, \delta, \pi_0, \pi_x, x^\mu} \rangle$$

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$$\Pi_\phi(x^0, x^i) \equiv \langle \sigma_{\epsilon, \delta, \pi_0, \pi_x, x^\mu} | \hat{\Pi}_\phi | \sigma_{\epsilon, \delta, \pi_0, \pi_x, x^\mu} \rangle$$

- number operator
- universe volume

$$\hat{N} = \int d^n \chi \int dg_I \hat{\varphi}^\dagger(g_I, \chi^a) \hat{\varphi}(g_I, \chi^a)$$

$$\hat{V} = \int d^n \chi \int dg_I dg'_I \hat{\varphi}^\dagger(g_I, \chi^a) V(g_I, g'_I) \hat{\varphi}(g'_I, \chi^a)$$

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• universe volume

$$\hat{V} = \int d^n \chi \int dg_I dg'_I \hat{\varphi}^\dagger(g_I, \chi^a) V(g_I, g'_I) \hat{\varphi}(g'_I, \chi^a)$$

• value of clock/rods scalar fields

$$\hat{X}^b \equiv \int d^n \chi \int dg_I \chi^b \hat{\varphi}^\dagger(g_I, \chi^a) \hat{\varphi}(g_I, \chi^a)$$

• momentum of clock/rods scalar fields

$$\hat{\Pi}_b = \frac{1}{i} \int d^n \chi \int dg_I \left[\hat{\varphi}^\dagger(g_I, \chi^a) \left(\frac{\partial}{\partial \chi^b} \hat{\varphi}(g_I, \chi^a) \right) \right]$$

note: dependence on matter scalar field data left implicit

used to define collective relational observables for effective continuum dynamics

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$$\hat{V} = \int d^n \chi \int dg_I dg'_I \hat{\varphi}^\dagger(g_I, \chi^a) V(g_I, g'_I) \hat{\varphi}(g'_I, \chi^a)$$

• value of clock/rods scalar fields

$$\hat{X}^b \equiv \int d^n \chi \int dg_I \chi^b \hat{\varphi}^\dagger(g_I, \chi^a) \hat{\varphi}(g_I, \chi^a)$$

• momentum of clock/rods scalar fields

$$\hat{\Pi}_b = \frac{1}{i} \int d^n \chi \int dg_I \left[\hat{\varphi}^\dagger(g_I, \chi^a) \left(\frac{\partial}{\partial \chi^b} \hat{\varphi}(g_I, \chi^a) \right) \right]$$

note: dependence on matter scalar field data left implicit

• value of matter scalar field

$$\hat{\Phi} = \frac{1}{i} \int dg_I \int d^4 \chi \int d\pi_\phi \hat{\varphi}^\dagger(g_I, \chi^\mu, \pi_\phi) \partial_{\pi_\phi} \hat{\varphi}(g_I, \chi^\mu, \pi_\phi)$$

• momentum of matter scalar field

$$\hat{\Pi}_\phi = \int dg_I \int d^4 \chi \int d\pi_\phi \pi_\phi \hat{\varphi}^\dagger(g_I, \chi^\mu, \pi_\phi) \hat{\varphi}(g_I, \chi^\mu, \pi_\phi)$$

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Effective volume and scalar matter dynamics: homogeneous background

Effective volume and scalar matter dynamics: homogeneous background

background volume dynamics:

L. Marchetti, DO, '21

A. Jercher, DO, A. Pithis, 21

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Effective volume and scalar matter dynamics: homogeneous background

background volume dynamics:

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e.g. (large density) if one spin mode dominates, and for such mode $\mu_{v_o}(\pi_\phi) \simeq c_{v_o} \pi_\phi$

and we consider states peaked on a given value of the matter scalar field momentum, we get

$$\mathcal{H}^2 \equiv \left(\frac{\bar{V}'}{3\bar{V}}\right)^2 = \frac{4}{9} \mu_{v_o}^2(\tilde{\pi}_\phi) = \frac{4\pi G}{3} \tilde{\pi}_\phi^2, \quad \mathcal{H}' = 0$$

i.e. the relational Friedmann eqns with scalar matter of momentum $\tilde{\pi}_\phi \equiv \bar{\Pi}_\phi^2 / \bar{N}^2$

and effective Newton constant $4c_{v_o}^2 = 12\pi G$

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- can also compute relative fluctuations in volume (etc): generically small - semiclassical limit is robust

L. Marchetti, DO, '20

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background volume dynamics:

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- quantum bounce at early times
- behaviour at small (relational) times, assuming conditions of "good relational clock" are satisfied:
 - there are solutions with singular behaviour (cosmological singularity not always resolved)
 - if at least one coefficient Q or at least one "energy" coefficient is non-zero:

 $\exists j / \rho_j(\chi) \neq 0 \forall \chi$ 

$V = \sum_j V_j \rho_j^2$
remains positive at all times
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quantum bounce (solving
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quantum bounce (solving classical singularity)!

- quantum fluctuations remain small also at bounce, for specific range of parameters (i.e. specific class of quantum states)

L. Marchetti, DO, '20

Inclusion of GFT interactions: phantom dark energy + asymptotic deSitter regime

M. De Cesare, A. Pithis, M. Sakellariadou, '16; DO, X. Pang, '21

Inclusion of GFT interactions: phantom dark energy + asymptotic deSitter regime

M. De Cesare, A. Pithis, M. Sakellariadou, '16; DO, X. Pang, '21

- phenomenological approach: consider general interactions

$$\mathcal{V}(\sigma, \bar{\sigma}) = - \sum_j \left(m_j^2 |\sigma_j|^2 + \frac{2\lambda_j}{n_j} |\sigma_j|^{n_j} + \frac{2\mu_j}{n'_j} |\sigma_j|^{n'_j} \right) \quad 2 < n_j < n'_j \quad |\mu_j| \ll |\lambda_j| \ll m^2$$

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$$w = 3 - \frac{2VV''}{(V')^2}$$

in terms of equation of state
for effective "matter content"

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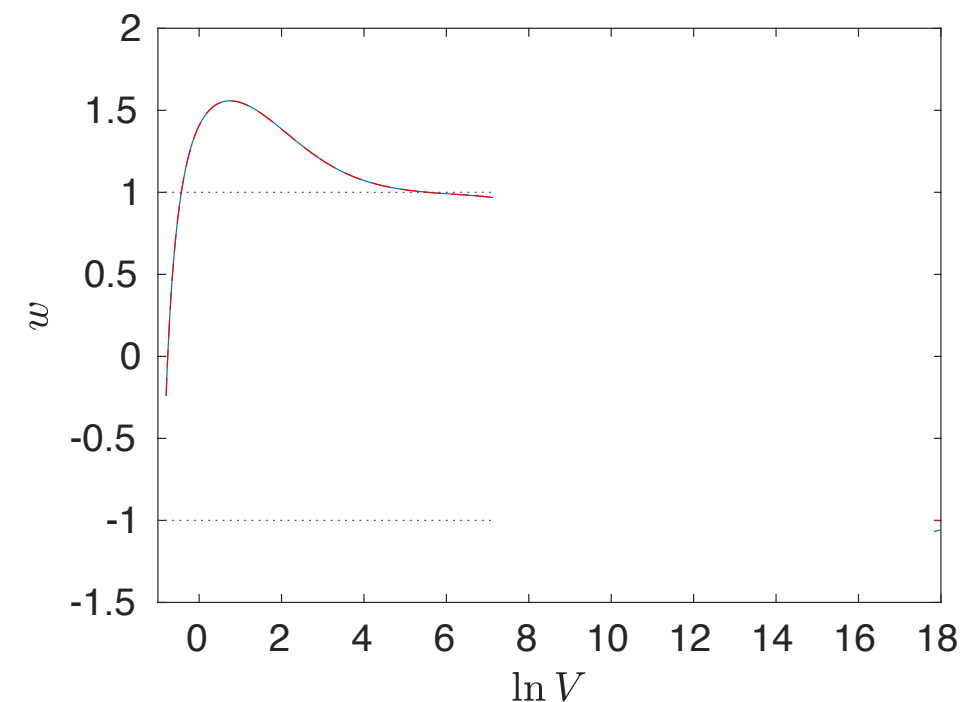
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Inclusion of GFT interactions: phantom dark energy + asymptotic deSitter regime

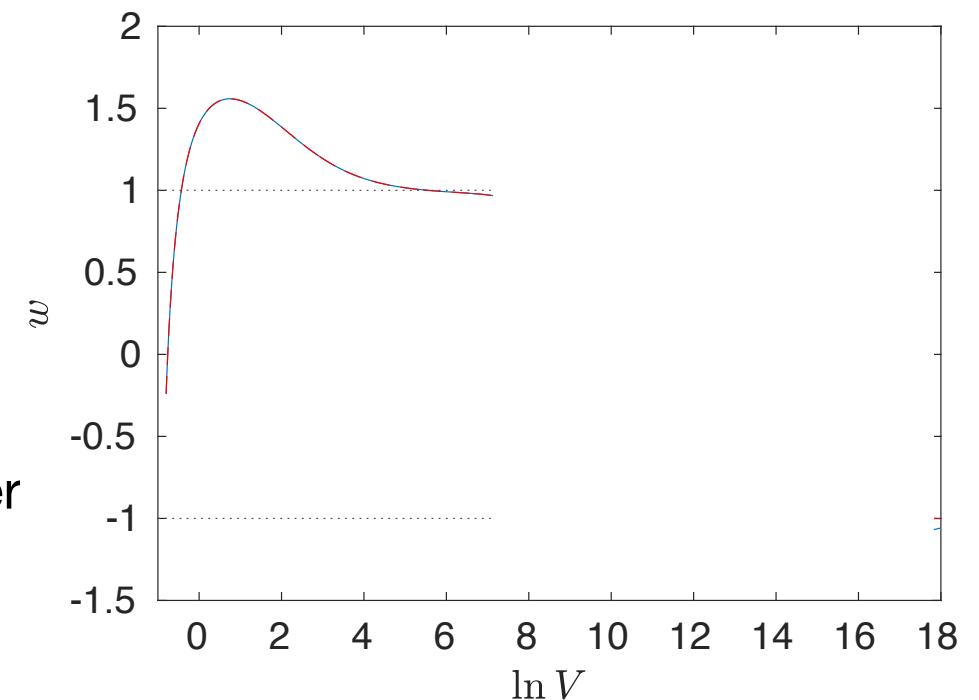
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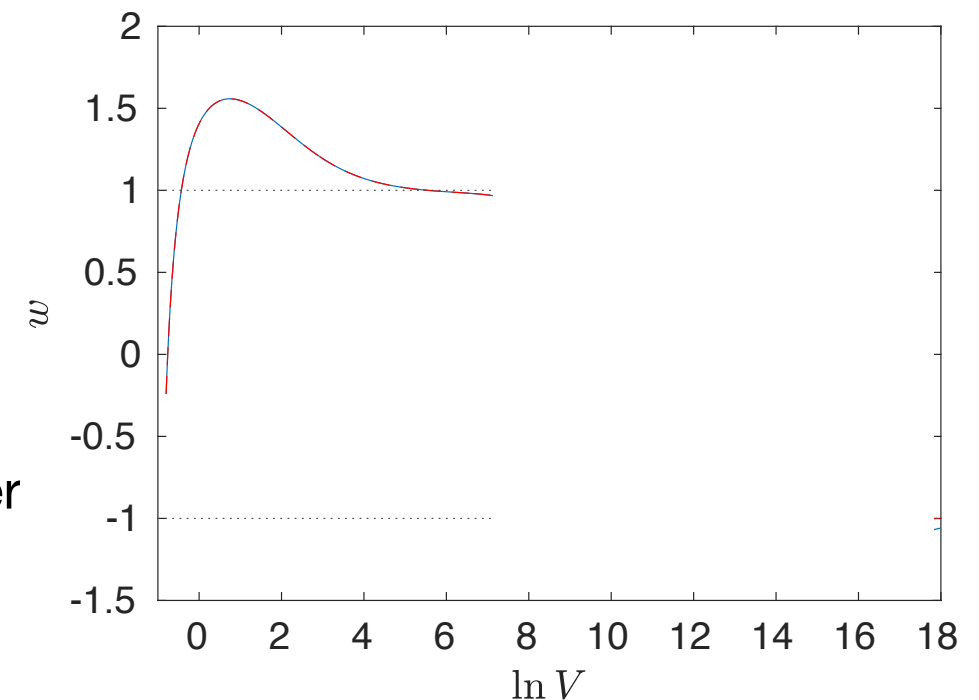
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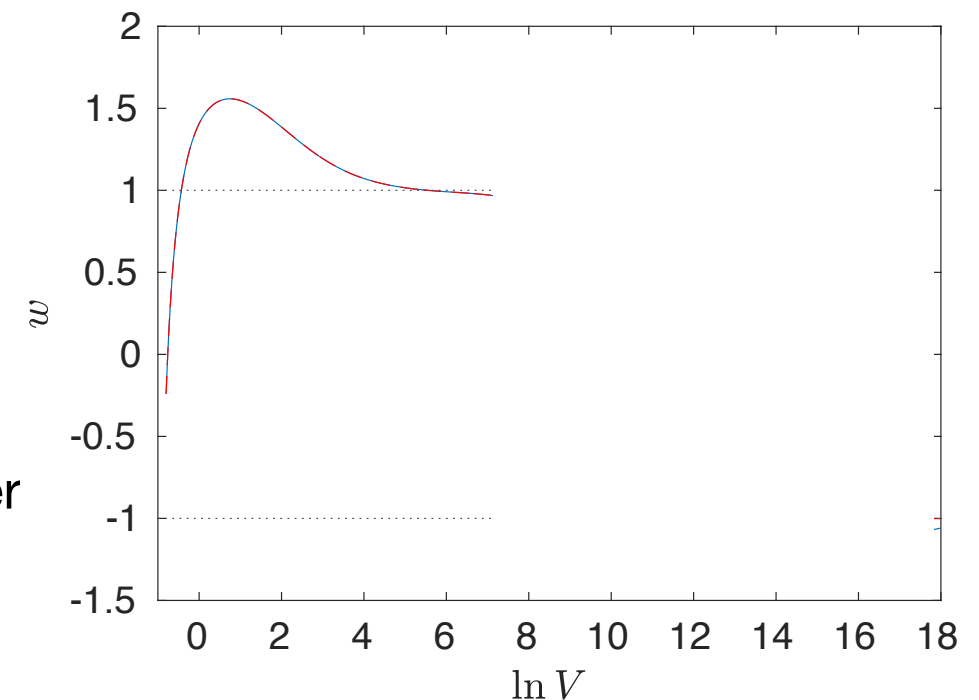
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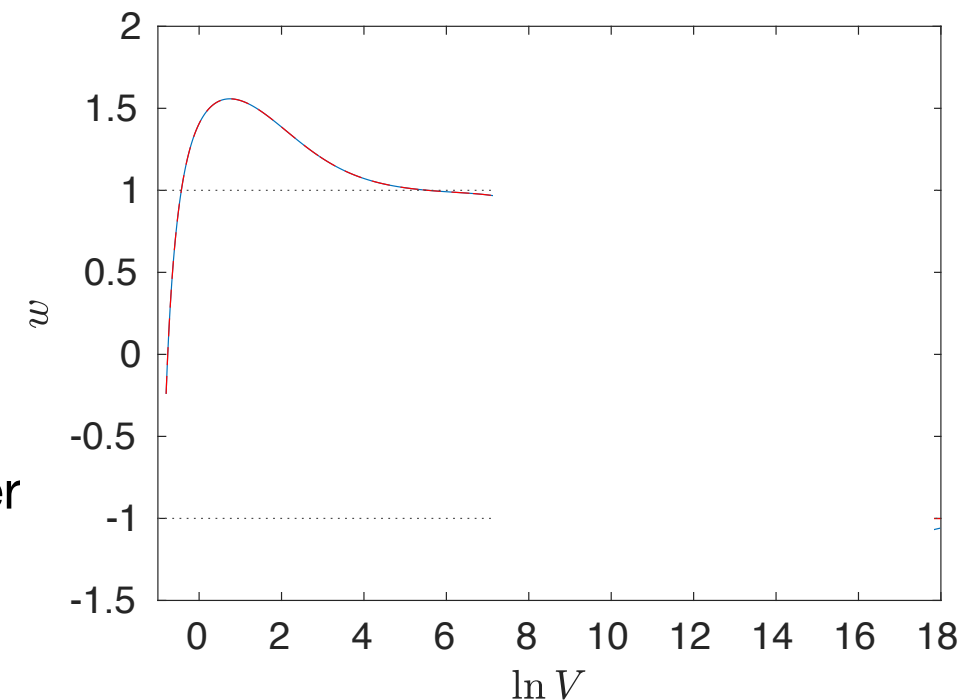
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$$\longrightarrow w = 2 - \frac{n}{2} - \left(\frac{n}{2} + 1 \right) \frac{V_1 V_2 r^2 \left(\sqrt{-\lambda_2} r^{n/2-1} - \sqrt{-\lambda_1} \right)^2}{\left(\sqrt{-\lambda_1} V_1 + \sqrt{-\lambda_2} V_2 r^{n/2+1} \right)^2} \quad r = \rho_2 / \rho_1$$

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- restrict attention to single interaction (appropriate at very late times/large volumes)

- late time evolution:

$$w = 2 - \frac{n}{2} - \left(\frac{n}{2} + 1 \right) \frac{V_1 V_2 r^2 \left(\sqrt{-\lambda_2} r^{n/2-1} - \sqrt{-\lambda_1} \right)^2}{\left(\sqrt{-\lambda_1} V_1 + \sqrt{-\lambda_2} V_2 r^{n/2+1} \right)^2} \quad r = \rho_2 / \rho_1$$

- one sees that: $w \leq 2 - \frac{n}{2}$ maximum is reached from below for large volumes (one mode dominates)

Inclusion of GFT interactions: phantom dark energy + asymptotic deSitter regime

M. De Cesare, A. Pithis, M. Sakellariadou, '16; DO, X. Pang, '21

- phenomenological approach: consider general interactions

$$\mathcal{V}(\sigma, \bar{\sigma}) = - \sum_j \left(m_j^2 |\sigma_j|^2 + \frac{2\lambda_j}{n_j} |\sigma_j|^{n_j} + \frac{2\mu_j}{n'_j} |\sigma_j|^{n'_j} \right) \quad 2 < n_j < n'_j \quad |\mu_j| \ll |\lambda_j| \ll m^2$$

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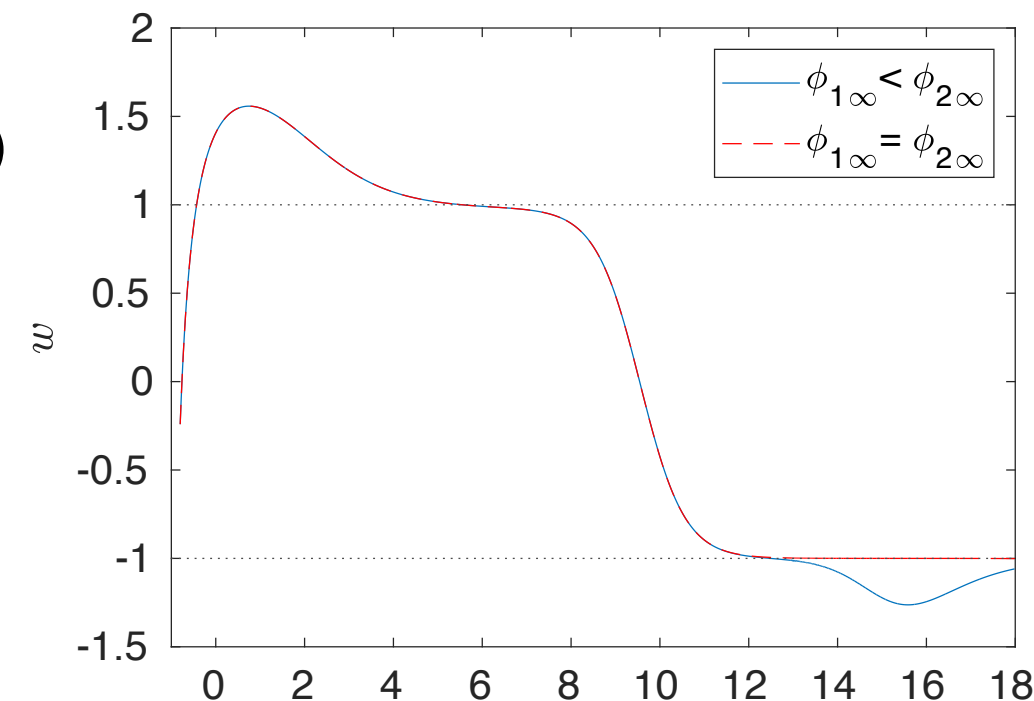
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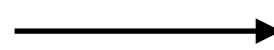
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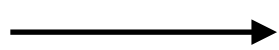
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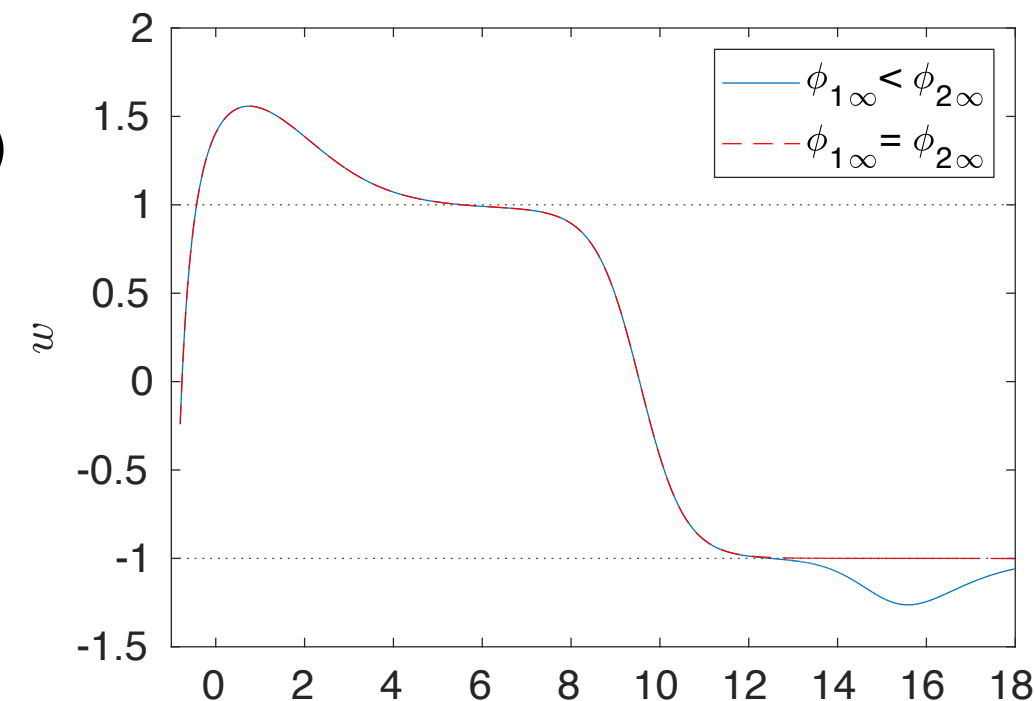


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- the energy density of the effective phantom field approaches a (cosmological) constant



asymptotically de Sitter universe



cosmological perturbations

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