RESEARCH STATEMENT

Diego Alejandro Mejía Guzmán

My main interests in the area of set theory are forcing theory and descriptive set theory. Also, I am deeply interested in the relation between set theory, analysis and topology, especially in obtaining consistency results on these areas.

In my first year as a doctoral student I have been studying applications of forcing to obtain consistency results about cardinal invariants, especially in the case when the continuum is large. Recently, using results about properties preserved in finite support iterations of c.c.c. forcing (see [3], [5] and [7]) and matrix iterations (see [4] and [2]), I have obtained consistency results about Cichon's diagram using several distinct values.

Other particular problem I am interested in is getting models with many distinct cardinal invariants parameterized by reals, like those presented in [6], [8], [9] and [10].

References

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