

## CURRICULUM VITAE

Nicolas Ressayre  
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born 27 decembre 1973  
Married, 3 sons  
Professor  
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### TITLES AND DIPLOMAS

- 2007 Habilitation to Supervise Research
- 2000 PhD from Université Grenoble 1.
- 1996 Aggregation of Mathematics (4th).  
DEA (mention TB).
- 1993 Entry at the Ecole Normale Supérieure de Lyon.

### PROFESSIONAL EXPERIENCE

- Dec 2011... Full professor at Université Lyon 1.
- 2001-2011 Maître de conférences at Université Montpellier II.
- 2000-01 Postdoctoral fellow at the University of Geneva.
- 1997-1998 Military service.
- 1997 and 99 PhD student at Université Grenoble 1.
- 1993-1996 Schooling at ENS Lyon.

### RESEARCH ANIMATION

- Funding ANR GeoLie project leader from 2015 to 2020  
IUF contract from 2012 to 2018
- Locally Member of committees for recruitment or promotions, organizer of seminars or working groups...  
Head of the Algebra-Geometry-Logic team of the ICJ since May 2018.  
Team with 53 members. Writing of the HCERES report, Organization of the team day, Profiles for job applications, Member of the management committee and the scientific committee of the laboratory
- Conferences Organization of the rotating colloquium on the theory of representations in 2004  
Organization of the Sophus Lie Seminar in 2013  
Organization of a thematic half-term of the Labex MiLyon in 2014  
Organization of the international conference « Algebraic groups: Geometry, Actions and Structures » in 2018 in Lyon  
Organization of the AGL team day in Lyon in 2019  
Organization of the summer school « Immeubles et Grassmanniennes affines » for 2 weeks in Luminy in 2019.
- Expertise Member of the editorial board of Asterisk  
Referee for many journals  
Reporter for ANR, ERC and NSA projects  
Reporter on teacher-researcher applications for foreign universities  
Member of the Scientific Committee of Cofund MathInParis2020

- Supervision Co-supervision with L. Manivel of Michael Lebarbier's thesis defended in 2009.  
 Supervision of Maxime Pelletier's thesis defended in 2017.  
 Co-supervision with K. Iohara of Khanh NGuyen's thesis from 2017 to 2021.  
 Supervision of Luca Francone's thesis 2021-2024.  
 Uffe Jorgensen, thesis student under the supervision of Niels Lauritzen did a 6-month internship in Montpellier in 2012.
- Jury Reviewer for five PhD, participation in 11 thesis juries and 3 HDR juries
- Collaborations 7 co-authors from my laboratory, 2 national collaboration (L. Manivel, PE Chapat) and 7 American co-authors (P. Belkale, S. Gao, S. Kumar, J. Landsberg, G. Orelowitz, E. Richmond, A. Yong).

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## PEDAGOGICAL RESPONSIBILITIES

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- 2014 -2018 President of the training commission of the DEM of Lyon 1 (number 2 of the department). Management of services, recruitment of ACEs, numerous temporary staff, drafting of a model, management of current affairs, replacement of the director in the event of his absence. . .
- 2013 - Elected member of the DEM council of Lyon 1.
- 2023 – Responsible for the implementation of the assessment by skills for the DEM
- 2005-2010 Member of the office of the teaching department in Montpellier.
- 2005-2009 Member of various reflection committees on teaching in Montpellier.
- 2008-2010 Responsible for the MFA course of the license of Montpellier.
- 2003-2004 Responsible for the preparation for the aggregation in Montpellier.

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## CENTRAL FUNCTIONS

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- 2019 – 2023 Elected member of the council of the Faculty of Sciences
- 2018 – Member of the ethics committee of the University Lyon 1
- 2014 – 2018 As number 2 of the mathematics department regular participations in various central councils of the University Lyon 1
- 2013 – 2018 Elected member of the council of the Faculty of Sciences and Technology of the University of Lyon 1

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## HONORS

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- ICM 2014 Invited speaker in the session « Lie Theory and Generalizations » .
- IUF 2012 Junior member of the Institut Universitaire de France.
- Bourbaki On November 11, 2011, Michel Brion presented work by Belkale, Kumar and myself at the Bourbaki seminar.
- 2012 Eligible on ERC starting Grants project

## PERSONAL BIBLIOGRAPHY

### Articles

1. *Newell-Littlewood numbers III: The saturated cone*,  
Shiliang Gao, Gidon Orelowitz, , **Nicolas Ressayre** et Alexander Yong.  
To appear in COMPOSITIO MATHEMATICA, 21pp.
2. *On the faces of the tensor cone of symmetrizable Kac-Moody Lie algebras*,  
Shrawan Kumar, **Nicolas Ressayre**  
To appear in ANN. SCI. ENS, 50 pp.
3. *On the multiplicity spaces of spherical subgroups of minimal rank*,  
Luca Francone, **Nicolas Ressayre**  
BULLETIN OF THE LONDON MATH SOCIETY, **55** (2023), no. 6, 2660–2684.
4. *On the automorphisms of the Drinfel'd double of a Borel Lie subalgebra*,  
Michaël Bulois, **Nicolas Ressayre**  
JOURNAL OF ALGEBRA **47** (2024), 515–532.
5. *Reductions for branching coefficients*,  
Pierre-Emmanuel Chaput, **Nicolas Ressayre**  
IMRN, (2023), no. 17, 15207–15265.
6. *Some unexpected properties of Littlewood-Richardson coefficients*,  
Maxime Pelletier, **Nicolas Ressayre**  
ELECTRON. J. COMBIN. 29 (2022), no. 4, Paper No. 4.11, 25 pp.
7. *On the tensor semigroup of affine Kac-Moody Lie algebras*,  
**Nicolas Ressayre**  
JOURNAL OF THE AMS, **35** (2022), no. 2, 309–360.
8. *Combinatorics of Newell-Littlewood numbers*,  
Shiliang Gao, Gidon Orelowitz, , **Nicolas Ressayre** and Alexander Yong.  
SÉM. LOTHAR. COMBIN. , **86B** (2022), Art. 18, 12pp.
9. *Reductions for branching coefficients*,  
**Nicolas Ressayre**  
J. LIE THEORY, **31** (2021), no. 3, 885–896.
10. *Vanishing symmetric Kronecker coefficients*,  
**Nicolas Ressayre**  
BEITRÄGE ZUR ALGEBRA UND GEOMETRIE / CONTRIBUTIONS TO ALGEBRA AND GEOMETRY, **61** (2020), no. 2, 231–246.
11. *Horn inequalities for nonzero Kronecker coefficients*,  
**Nicolas Ressayre**  
ADVANCES IN MATH., **356** (2019), 21pp.
12. *Permanent v. determinant: An exponential lower bound assuming symmetry and a potential path towards Valiant's conjecture*,  
Joseph Landsberg, **Nicolas Ressayre**  
DIFFERENTIAL GEOMETRY AND ITS APPLICATIONS, **55** (2017), 146–166.

13. *Distribution on homogeneous spaces and Belkale-Kumar's product*,  
**Nicolas Ressayre**  
PROGR. MATH., 326, 481 – 526, Birkhäuser/Springer, Cham, 2018.
14. *Permanent v. determinant: an exponential lower bound assuming symmetry [extended abstract]*,  
Joseph Landsberg, **Nicolas Ressayre**  
ITCS'16 – PROCEEDINGS OF THE 2016 ACM CONFERENCE ON INNOVATIONS IN THEORETICAL COMPUTER SCIENCE, 29–35, ACM, New York, 2016.
15. *Generalisations of the PRV conjecture II*,  
Pierre-Louis Montagard et Boris Pasquier, **Nicolas Ressayre**  
J. PURE APPL. ALGEBRA, **219** (2015), no. 12, p. 5560 – 5572
16. *The saturation property for branching rules – Examples*,  
Boris Pasquier, **Nicolas Ressayre**  
EXPERIMENTAL MATHEMATICS, **22** (3), p. 1–22, 2013.
17. *A generalization of the Fulton conjecture for arbitrary groups*,  
P. Belkale, S. Kumar et **N. Ressayre**  
MATHEMATISCHE ANNALEN, **354**, Pp. 401–425, 2012.
18. *Two generalizations of the PRV conjecture*,  
PL. Montagard, B. Pasquier, **N. Ressayre**  
COMPOSITIO MATHEMATICA, **147** (04), pages 1321–1336, 2011.
19. *Multiplicative formulas in Cohomology of  $G/P$  and in quiver representations*,  
**Nicolas Ressayre**  
INDAG. MATH., **22**(1-2), p. 87–102, 2011.
20. *Hypersurfaces with degenerate duals and the Geometric Complexity Theory Program*,  
J. Landsberg, L. Manivel, **Nicolas Ressayre**  
COMMENTARII MATH HELV. , **88** (2), pages 469–484, 2011.
21. *A cohomology free description of eigencones in type A, B and C*,  
**Nicolas Ressayre**  
INTERNATIONAL MATH RESEARCH NOTICES (IMRN), **2012**, Issue 21, Pp. 4966–5005, 2012.
22. *A short geometric proof of a conjecture of Fulton*,  
**Nicolas Ressayre**  
ENS. MATH (2), **57**, pages 103-115, 2011.
23. *GIT-cones and quivers*,  
**Nicolas Ressayre**  
MATHEMATISCHE ZEITSCHRIFT (online first), pages 1–13, 2011.
24. *Geometric Invariant Theory and Generalized Eigenvalue Problem II*,  
**Nicolas Ressayre**  
ANNALES DE L'INSTITUT FOURIER, **61** (4), p. 1467–1491, 2011.
25. *Branching Schubert Calculus and Belkale-Kumar Product on Cohomology*,  
Edward Richmond, **Nicolas Ressayre**  
PROC. AMS, **139**, pages 835-848, 2011.

26. *Geometric Invariant Theory and Generalized Eigenvalue Problem*,  
**Nicolas Ressayre**  
INVENTIONES MATHEMATICAE, **180**, pages 389–441, 2010.
27. *Spherical homogeneous spaces of minimal rank*,  
**Nicolas Ressayre**  
ADVANCES IN MATH, **224**, issue 5, pages 1784–1800, 2010.
28. *Lattice Polytopes and Root Systems*,  
Pierre-Louis Montagard, **Nicolas Ressayre**  
BULL. LONDON MATH SOCIETY, **41**(2), pages 227–241, 2009.
29. *Invariant deformations of orbit closures in  $\mathfrak{sl}(n)$* ,  
S Jansou, **Nicolas Ressayre**  
REPRESENTATION THEORY, **13**, pages 50–62, 2009.
30. *Sur des faces du LR-cône généralisé*,  
Pierre-Louis Montagard, **Nicolas Ressayre**  
BULLETIN DE LA SMF **135**, no. 3, pages 343–365, 2007.
31. *Adjacency of Young tableaux and the Springer fibers*,  
Jean Pagnon, **Nicolas Ressayre**  
SELECTA MATHETICA, NEW SERIES, **12**, no. 3-4, pages 517–540, 2006.
32. *About Knop’s action of the Weyl group on the set of orbits of a spherical subgroup in the flag manifold*,  
**Nicolas Ressayre**  
TRANSFORMATION GROUPS, **10**, no. 2, pages 255–265, 2005.
33. *Balanced configurations of  $2n + 1$  plane vectors*,  
**Nicolas Ressayre**  
JOURNAL OF COMBINATORICS ALGEBRA, **21**, no. 3, pages 281–287, 2005.
34. *A quadratic born for the Determinant and Permanent problem*,  
Thierry Mignon, **Nicolas Ressayre**  
INTERN. MATH RESEARCH NOTICES (IMRN), **79**, pages 4241–4254, 2004.
35. *Sur les orbites d’un sous-groupe sphérique dans la variété des drapeaux*,  
**Nicolas Ressayre**  
BULLETIN DE LA SMF, **132**, pages 543–567, 2004.
36. *Quotients of group completions by spherical subgroups*,  
**Nicolas Ressayre**  
J. OF ALGEBRA, **265**, pages 1–44, 2003.
37. *The GIT-equivalence for  $G$ -line bundles*,  
**Nicolas Ressayre**  
GEOM. DEDICATA, **81** no.1-3, 295–324, 2000.
38. *Appendix: an example of a thick wall*,  
**Nicolas Ressayre**  
PUB. MATH. IHES, **87** 53–56, 1998, Appendix to a Dolgachev-Hu’s paper.

## Submitted Preprints

39. *Intersection multiplicity one for the Belkale-Kumar product in  $G/B$ ,*  
Luca Francone, **Nicolas Ressayre**.
40. *Bidilation of small Littlewood-Richardson coefficients,*  
Pierre-Emmanuel Chaput, **Nicolas Ressayre**. To appear in REPRESENTATION THEORY.

### **Preprints**

41. *A parametric non generic Richardson variety in the cominuscle case,*  
Pierre-Emmanuel Chaput, **Nicolas Ressayre**.

### **In Preparation**

42. *An Algorithm to compute the Kronecker cone,*  
Bulois Micahel, Denis Roland, **Nicolas Ressayre**.
43. *On relative semi-stability,*  
Paul-Emile Paradan, **Nicolas Ressayre**.
44. *The moment cone of an affine  $G$ -variety,*  
Paul-Emile Paradan, **Nicolas Ressayre**.
45. *The moment cone of an affine  $G$ -variety with involution,*  
Paul-Emile Paradan, **Nicolas Ressayre**.

## THE 5 MOST SIGNIFICANT PUBLICATIONS

1. *Tensor semigroup of affine KM Lie algebras*,  
 JOURNAL OF THE AMS, **35** (2022), no. 2, 309–360.

Abstract: In this work, we prove a Brown-Kumar conjecture that describes the asymptotic support of the decomposition of the tensor product of integrable representations of highest weight for an affine Kac-Moody algebra.

In my opinion, three factors make this work valuable: 1- We introduce a new method to study the very classical Horn problem. A method that allows us to redemonstrate without using the Hilbert-Mumford theorem or the notion of semi-stability, the description of the Horn cone for the group  $U_n(\mathbb{C})$ . 2- The infinite dimension induces significant technical complications that had to be overcome. 3- We solve a Kumar conjecture on a subject for which he is recognized as the world specialist.

As a bonus, we exhibit, for each type, an explicit saturation constant. In finite dimension, the semigroup, support of the tensor product, is of finite type, ensuring the existence, a priori, of such constants. For an affine algebra, this existence was not assured a priori.

2. *On the faces of the tensor cone of symmetrizable Kac-Moody Lie algebras*, With Shrawan Kumar  
 To appear in ANN. SCI. ENS, 50 pp.

Abstract: We show here that each inequality of the Brown-Kumar conjecture induces a codimension one face of the tensor cone for any symmetrizable Kac-Moody algebra. If the general approach follows my proof published in *Inventiones* in the case of finite-dimensional algebras, the infinite dimension induces considerable complications in the geometric arguments.

3. *A generalization of the Fulton conjecture for arbitrary groups*,  
 with P. Belkale et S. Kumar  
 MATHEMATISCHE ANNALEN, 354 (2), pages 401-4251, 2012.

Abstract: Given three partitions  $\lambda$ ,  $\mu$  and  $\nu$ , we denote by  $c_{\lambda,\mu}^{\nu}$  the Littlewood-Richardson coefficient. On the one hand, these coefficients encode the decomposition of the tensor product of representations for the linear group. On the other hand, they are the structure coefficients of the cup product on the cohomology ring of Grassmannians. The following result had been conjectured by Fulton and was shown by Knutson-Tao:

$$c_{\lambda,\mu}^{\nu} = 1 \quad \Rightarrow \quad c_{n\lambda,n\mu}^{n\nu} = 1,$$

for any positive integer  $n$ .

We show here a generalization of this conjecture that relates the theory of the intersection of any flag variety to the multiplicities of the decomposition of tensor products. Let  $G$  be a complex semisimple group,  $P$  a parabolic subgroup of  $G$  and  $L$  a Levi subgroup of  $P$ . More precisely, we show that if a Levi-mobile structure coefficient of the cohomology of  $G/P$  is equal to one then a half-line of multiplicities for the decomposition of the tensor product of simple  $L$ -modules is equal to one.

In the case where  $G$  is equal to  $SL_n$ , we thus obtain a new proof of Fulton's conjecture, in which the two interpretations of the Littlewood-Richardson coefficients play very different roles.

4. *Two generalizations of the PRV conjecture*,  
with Pierre-Louis Montagnard et Boris Pasquier,  
COMPOSITIO MATHEMATICA, 147 (04), pages1321–1336, 2011.

Abstract: Let  $G$  be a reductive and connected complex group. The PRV conjecture, which was proved independently in 1989 by S. Kumar and O. Mathieu, provides explicit irreducible submodules in the tensor product of two simple  $G$ -modules. More precisely, let  $V_G(\mu)$  and  $V_G(\nu)$  be two simple  $G$ -modules of highest weights  $\mu$  and  $\nu$  respectively. Then, for any element  $w$  of the Weyl group  $W$  of  $G$ , the simple  $G$ -module  $V_G(\overline{\mu + w\nu})$  of highest weight  $\mu + w\nu$  appears with multiplicity at least one in  $V_G(\mu) \otimes V_G(\nu)$ .

This paper achieves three goals. First, we simplify Shrawan Kumar's proof of the PRV conjecture. We also generalize the PRV conjecture to other restriction problems. Finally, we improve the PRV conjecture by explaining new components of  $V_G(\mu) \otimes V_G(\nu)$ .

5. *Geometric Invariant Theory and the Generalized Eigenvalue Problem*,  
INVENTIONES MATHEMATICAE, 180, pages 389–441, 2010.

Abstract: Let  $G$  be a connected reductive subgroup of a complex and reductive connected group  $\hat{G}$ .

Let us fix maximal tori and Borel subgroups of  $G$  and  $\hat{G}$  such that the irreducible modules are parametrized by their highest weights. The pairs  $(\nu, \hat{\nu})$  of dominant weights such that  $V_G(\nu)^*$  is a submodule of  $V_{\hat{G}}(\hat{\nu})$  form a monoid of finite type. The description of the polyhedral convex cone  $\mathbb{Q}_{\geq 0}\mathcal{S}(G, \hat{G})$  generated by this semigroup is a very rich subject whose history goes back to a work by Herman Weyl in 1912.

Here we describe the minimal set of inequalities that characterizes the cone  $\mathbb{Q}_{\geq 0}\mathcal{S}(G, \hat{G})$  as a part of the dominant chamber. In other words, we bijectively parameterize the codimension 1 faces of  $\mathbb{Q}_{\geq 0}\mathcal{S}(G, \hat{G})$  that meet the interior of the dominant chamber.

The obtained proof of the minimality of the list of inequalities is our major result here. The only previously known case was that of the tensor product for the linear group which had been shown 6 years before by Knutson-Tao-Woodward with totally different methods.